

Comp 311

Functional Programming

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Announcements

- Homework 2 Available from Piazza (Due October 1)
- Two Sigma Info Session at Huff House, 4pm Today

Traversing Multiple Recursive Datatypes

Taking the First Few Elements

```
def take(n: Nat, xs: List): List = {  
  // require n <= size(xs)  
  (n, xs) match {  
    case (Zero, xs) => Empty  
    case (Next(m), Cons(y, ys)) => Cons(y, take(m, ys))  
  }  
}
```

Taking the First Few Elements

```
def take(n: Int, xs: List): List = {  
  require ((n >= 0) && (n <= size(xs)))  
  (n, xs) match {  
    case (0, xs) => Empty  
    case (n, Cons(y, ys)) => Cons(y, take(n-1, ys))  
  }  
}
```

Dropping the First Few Elements

```
def drop(n: Int, xs: List): List = {  
  require (n <= size(xs))  
  (n, xs) match {  
    case (0, xs) => xs  
    case (n, Cons(y, ys)) => drop(n-1, ys)  
  }  
}
```

Functional Update of a List

```
def update(xs: List, i: Nat, y: Int): List = {  
  require (xs != Empty) // && i < size(xs)  
  
  (xs, i) match {  
    case (Cons(z, zs), Zero) => Cons(y, zs)  
    case (Cons(z, zs), Next(j)) => Cons(z, update(zs, j, y))  
  }  
}
```

Functional Update of a List

```
def update(xs: List, i: Int, y: Int): List = {  
  require ((i >= 0) && (i < size(xs)))  
  assert (xs != Empty)  
  
  (xs, i) match {  
    case (Cons(z, zs), 0) => Cons(y, zs)  
    case (Cons(z, zs), _) => Cons(z, update(zs, i-1, y))  
  }  
}
```


Design Abstraction

Our Function Templates Reveal Common Structure

```
def containsZero(xs: List): Boolean = {  
  xs match {  
    case Empty => false  
    case Cons(n, ys) => (n == 0) || containsZero(ys)  
  }  
}
```

```
def containsOne(xs: List): Boolean = {  
  xs match {  
    case Empty => false  
    case Cons(n, ys) => (n == 1) || containsOne(ys)  
  }  
}
```

Our Function Templates Reveal Common Structure

```
def contains(m: Int, xs: List): Boolean = {  
  xs match {  
    case Empty => false  
    case Cons(n, ys) => (n == m) || contains(m, ys)  
  }  
}
```

But Sometimes the Part We Want to Abstract Is a Function

```
def below(m: Int, xs: List): List = {  
  xs match {  
    case Empty => Empty  
    case Cons(n, ys) => {  
      if (n < m) Cons(n, below(m, ys))  
      else below(m, ys)  
    }  
  }  
}
```

But Sometimes the Part We Want to Abstract Is a Function

```
def above(m: Int, xs: List): List = {  
  xs match {  
    case Empty => Empty  
    case Cons(n, ys) => {  
      if (n > m) Cons(n, above(m, ys))  
      else above(m, ys)  
    }  
  }  
}
```

Taking Functions As Parameters

```
def filter(f: (Int)=>Boolean, xs: List): List = {  
  xs match {  
    case Empty => Empty  
    case Cons(n, ys) => {  
      if (f(n)) Cons(n, filter(f, ys))  
      else filter(f, ys)  
    }  
  }  
}
```

Passing Functions as Arguments

```
val xs = Cons(1, Cons(2, Cons(3, Cons(4, Cons(5, Cons(6, Empty))))))
```

```
filter(((n: Int) => (n > 0)), xs) ↦*  
Cons(1, Cons(2, Cons(3, Cons(4, Cons(5, Cons(6, Empty))))))
```

```
filter(((n: Int) => (n < 0)), xs) ↦*  
Empty
```

```
filter(((n: Int) => (n < 3)), xs) ↦*  
Cons(1, Cons(2, Empty))
```

Passing Functions as Arguments

```
val xs = Cons(1, Cons(2, Cons(3, Cons(4, Cons(5, Cons(6, Empty))))))
```

```
filter(((n: Int) => (n > 0))), xs) ↦*  
Cons(1, Cons(2, Cons(3, Cons(4, Cons(5, Cons(6, Empty))))))
```

```
filter(((n: Int) => (n < 0))), xs) ↦*  
Empty
```

```
filter(((n: Int) => (n < 3))), xs) ↦*  
Cons(1, Cons(2, Empty))
```

These are
function literals



First-Class Functions

- Function literals are expressions with static arrow types that reduce to *function values*
- The value type of a function value is also an arrow type
- Function values are first-class values:
 - They are allowed to be passed as arguments
 - They are allowed to be returned as results

Simplifying Function Literals

- Parameter types on function literals are allowed to be elided whenever the types are clear from context

```
filter((n: Int) => (n > 0)), xs)
```

can be written as

```
filter((n) => (n > 0)), xs)
```

Simplifying Function Literals

- Parentheses around a single parameter is allowed to be omitted

```
filter((n) => (n > 0)), xs)
```

can be written as

```
filter(n => (n > 0), xs)
```

Simplifying Function Literals

- When a single parameter is used only once in the body of a function literal:
 - We can drop the parameter list
 - We simply write the body with an `_` at the place where the parameter is used

For example,

```
((x: Int) => (x < 0))
```

becomes

```
_ < 0
```