Homework 5
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Due: 12 noon on Friday, April 22, 2016
with extension till noon on Monday, May 2, 2016.

All homeworks should be submitted in a directory named “hw_5” in your svn repository for this course. In case of problems committing your files, please contact the teaching staff at comp322-staff@rice.edu before the deadline to get help resolving for your issues. No late submissions will be accepted unless you are using your slip days.

The slip day policy for COMP 322 is similar to that of COMP 321. All students will be given 3 slip days to use throughout the semester. When you use a slip day, you will receive up to 24 additional hours to complete the assignment. You may use these slip days in any way you see fit (3 days on one assignment, 1 day each on 3 assignments, etc.). If you use slip days, you must submit a SLIPDAY.txt file in your svn homework folder before the actual submission deadline indicating the number of slip days that you plan to use.

The written report and the final project are due by the deadline for this homework. Other than slip days, no extensions will be given unless there are exceptional circumstances (such as severe sickness, not because you have too much other work). Such extensions must be requested and approved by the instructor (via e-mail, phone, or in person) before the due date for the assignment. Last minute requests are likely to be denied.

If you see an ambiguity or inconsistency in any homework question, please seek a clarification on Piazza or from the teaching staff. If it is not resolved through those channels, you should state the ambiguity/inconsistency that you see, as well as any assumptions that you make to resolve it.

Honor Code Policy: All submitted homeworks are expected to be the result of your individual effort. You are free to discuss course material and approaches to problems with your other classmates, the teaching assistants and the professor, but you should never misrepresent someone else’s work as your own. If you use any material from external sources, you must provide proper attribution.
1 Written Assignment: Locality with Places and Distributions (25 points)

The use of the HJlib place construct (Lecture 32) is motivated by improving locality in a computer system's memory hierarchy. We will use a very simple model of locality in this problem by focusing our attention on remote reads. A remote read is a read access on variable V performed by task T0 executing in place P0, such that the value in V read by T0 was written by another task T1 executing in place P1 ≠ P0. All other reads are local reads. By this definition, the read of A[0] in line 8 in the example code below is a local read and the read of A[1] in line 9 is a remote read, assuming this HJlib program is run with 2 places, each place with one worker thread.

1. finish {
2. place p0 = place(0); place p1 = place(1);
3. double[] A = new double[2];
4. finish {
5. async at(p0) { A[0] = ... ; } async at(p1) { A[1] = ... ; }
6. }
7. async at(p0) {
8. ... = A[0]; // Local read
9. ... = A[1]; // Remote read
10. }
11. }

Consider the following variant of the one-dimensional iterative averaging example studied in past lectures. We are only concerned with local vs. remote reads in this example, and not with the overheads of creating async tasks.

1. dist d = dist.factory.block([1:N]); // generate block distribution (Lecture 31)
2. for (point [iter] : [0:M-1]) {
3. finish for(int j=1; j<=N; j++)
4. async at(d[j]) {
5. myNew[j] = (myVal[j-1] + myVal[j+1]) / 2.0;
6. } //finish-for-async-at
7. double[] temp = myNew; myNew = myVal; myVal = temp;
8. } // for

1. (10 points) Write a formula for the total number of remote reads in this code as a symbolic function of the array size parameter, N, the number of iterations, M, and the number of places P (assuming that the HJlib program was executed using P places, and 1 worker thread per place).

2. (10 points) Repeat part 1 above if line 1 was changed to dist d = dist.factory.cyclic([1:N]);

3. (5 points) What conclusions can you draw about the relative impact of block vs. cyclic distributions on the number of remote reads in this example?

2 Written Assignment: Message Passing Interface (25 points)

Consider the MPI code fragment shown below when executed with two processes:

1. (10 points) What value will be output by the print statement in process 0?
2. **(15 points)** How will the output change if the Irecv() call is replaced by Recv() (and the Wait() call eliminated)?

```java
1. int rank, size, next, prev;
2. int n1[], n2[] = new int[1];
3. int tag1 = 201, tag2 = 202;
4. Request request; Status status;
5. size = MPI.COMM_WORLD.Size();
6. rank = MPI.COMM_WORLD.Rank();
7. next = (rank + 1) % size;
8. prev = (rank + size - 1) % size;
9. n1[0] = rank*10 + 1; n2[0] = rank*10 + 2;
10. if (rank == 0) {
11. request = MPI.COMM_WORLD.Irecv(n1, 0, 1, MPI_INT, prev, tag1);
12. MPI.COMM_WORLD.Send(n2, 0, 1, MPI_INT, next, tag2);
13. status = MPI.COMM_WORLD.Wait(request);
14. System.out.println("Output = " + n1[0]);
15. } else { // rank == 1
16. MPI.COMM_WORLD.Recv(n1, 0, 1, MPI_INT, prev, tag2);
17. n2[0] = n1[0];
18. MPI.COMM_WORLD.Send(n2, 0, 1, MPI_INT, next, tag1);
19. }
```

3 Programming Assignment *(50 points total)*

In the Actors lab, we used HJlib Actors to approximate \( \pi \). In the Message Passing Interface (MPI) lab, we will gain experience with distributed computing using MPI. The goal of this programming assignment is to exploit inter-process parallelism (by communicating using MPI) while computing \( \pi \).

3.1 **Pi Computation using Bailey-Borwein-Plouffe formula**

The assignment involves computing \( \pi \) to a specified precision using MPI. The following formula can be used to compute \( \pi \):

\[
\pi = \sum_{n=0}^{\infty} \left( \frac{4}{8n+1} - \frac{2}{8n+4} - \frac{1}{8n+5} - \frac{1}{8n+6} \right) \left( \frac{1}{16} \right)^n
\]

The PiNumTermsSerial.java file contains a simple sequential algorithm for computing \( \pi \) using Java’s BigDecimal data type, that runs for a fixed number of iterations. The PiNumTermsMpi.java file contains a parallel version of PiNumTermsSerial.java using MPI for inter-process communication and parallelism. The provided code includes implementations of the send*Message() and recv*Message() variants of communicating Java objects between the processes.

In contrast, the PiPrecisionSerial.java file contains a more realistic sequential algorithm that uses a while loop to compute more and more terms of the series until a desired precision is reached. **Your first task is to convert the sequential program in PiPrecisionSerial.java (for computing \( \pi \) to a desired precision) to a distributed parallel program in PiPrecisionMpi.java by using MPI for communication between the processes.** We have already provided a version of PiPrecisionMpi.java with TODO comments as helpful hints. Your task will include filling in code to address the comments in the TODO segments. Please do not modify the provided main() method in PiPrecisionMpi. The output produced by the main() method will be used to verify the correctness of your solutions.
The next task is to evaluate the performance of the serial and parallel versions, `PiPrecisionSerial` and `PiPrecisionMpi`, on a NOTS compute node. You are required to measure the speedup of your solution (`PiPrecisionMpi`) over the sequential implementation (`PiPrecisionSerial`) on NOTS while using $P$ processes for the following four values and using `precisionDigits = 25,000`:

1. $P = 1$,
2. $P = 2$,
3. $P = 4$ and

**Note:** Like lab 12, you will only be able to run your code on NOTS. It likely will not run locally. Local execution is not supported as this homework depends on compiled third-party binaries and a complex development environment that is only available on NOTS. However, you will still be able to compile locally as long as you import the project dependencies from the provided `pom.xml`.

### 3.2 Hints

- Passing individual terms to the helper processes from the main process will incur a lot of inter-process communication overhead. You may obtain performance benefits by sending ranges of terms (like chunking) to compute to the helper processes. These ranges can then be distributed among local worker actors to compute the sum of the corresponding terms.

- The `edu.rice.comp322.mpi.MpiUtils` class provides helpful methods to `send()` and `recv()` complex Java objects between the MPI processes. You may try and reduce the overhead in how `BigDecimal` instances are communicated across the processes. If so, you will need to create `send*Message()` and `recv*Message()` methods of your own while developing your solution in `PiPrecisionMpi`. You should, however, be able to reuse the existing `MpiUtils.ResultMessage` class.

- You will notice that there are no unit tests included in the project. The teaching staff will rely on running their reference solution and the sequential `PiPrecisionSerial` and comparing the console output (obtained from `System.out.println()` statements) to verify the correctness of the value of PI computed by your program.

### 3.3 Points distribution

- **[Solution correctness and efficacy (25 points)]** You will be graded on the correctness of your solution while extracting inter-process parallelism using MPI. Your coverage of the various TODOs and issues mentioned in the provided hints should help achieve the maximum points.

- **[Performance evaluation (10 points)]** You should include performance numbers for the four values of $P$ mentioned earlier in the document using `precisionDigits = 25,000`. For your reference purposes, our solution achieved over $3\times$ and over $5\times$ speedup over the sequential `PiPrecisionSerial` on 4 and 8 MPI processes, respectively. You can get these performance numbers using the provided SLURM script under `src/main/resources`.

- **[Homework report (15 points)]** You should submit a brief report summarizing the design and implementation of your solution, and explain why you believe that the implementation is correct, including why it is free of data races, deadlocks, and livelocks.

Please place the report file(s) in the top-level `hw5` directory. Remember to commit all your source code into the subversion repository during your assignment submission.