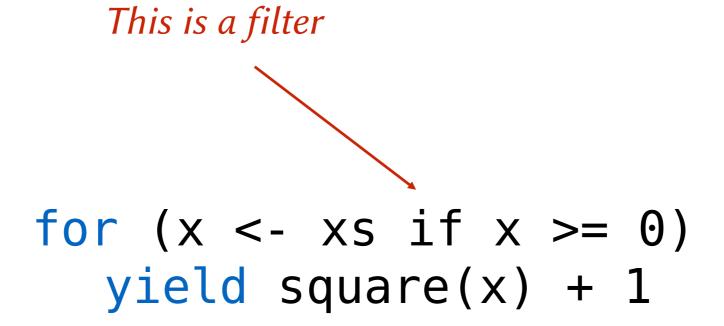
Comp 311 Functional Programming

Nick Vrvilo, Two Sigma Investments Robert "Corky" Cartwright, Rice University

October 17, 2017

Filters in For Expressions



Filters in For Expressions

- Filters are attached to generators
- A given generator can have zero or more filters

Filters in For Expressions

```
for (
    x <- xs
    if x >= 0
    if x % 2 == 0
) yield square(x) + 1
```

Clauses Can Be Enclosed in Braces Instead of Parentheses

```
for {
    x <- xs
    if x >= 0
    if x % 2 == 0
} yield square(x) + 1
```

For Expressions Can Include Multiple Generators

```
for {
    x <- xs
    if x >= 0
    y <- ys
    if y % 2 == 0
} yield x * y</pre>
```

For Expressions Can Include Local Bindings

```
for {
    x <- xs
    if x >= 0
    square = x * x
    y <- ys
    if y % square == 0
} yield x * y</pre>
```

Generators Can Specify Arbitrary Patterns

Generators Can Specify Arbitrary Patterns

- Elements of the collection that do not match the pattern are filtered
- Effectively, a pattern in a for expression serves as part of a generator and a filter

Guidelines on Using For Expressions

- Prefer for expressions to maps and filters
- They tend to be easier to read:
 - All bindings and collections iterated over are listed up front
- Prefer {...} to (...) around non-trivial for clauses

For vs Map

• Compare:

```
for (x <- xs if x >= 0)
  yield square(x) + 1
```

• To:

$$xs.filter(>= 0).map(square() + 1)$$

For Expressions and Database Queries

- for expressions are similar to standard database queries
- Consider a simple in-memory database of books, represented as a list of Book instances (Odersky et al 2012):

case class Book(title: String, authors: String*)

For Expressions and Database Queries

```
val books: List[Book] =
  Cons (
    Book (
      "Structure and Interpretation of Computer Programs",
      "Abelson, Harold", "Sussman, Gerald J."
    Book (
      "How to Design Programs",
      "Felleisen, Matthias", "Findler, Robert Bruce",
      "Flatt, Mathew", "Krishnamurthi, Shriram"
    Book (
      "Programming in Scala",
      "Odersky, Martin", "Spoon, Lex", "Venners, Bill"
```

Finding All Books Whose Author Has Last Name "Sussman"

```
for {
  b <- books
  a <- b.authors
  if a startsWith "Sussman,"
} yield b.title</pre>
```

Finding All Books That Have The String "Program" In the Title

```
for {
  b <- books
  if b.title indexOf "Program" >= 0
} yield b.title
```

Finding All Authors That Have Written More Than One Book in the Database

```
for {
   b1 <- books
   b2 <- books if b1 != b2
   a1 <- b1.authors
   a2 <- b2.authors
   if a1 == a2
} yield a1</pre>
```

Translating For Expressions

- For expressions are simply translated to maps, flatMaps, and filters by the Scala compiler
- Translation occurs before type checking
 - Why is this preferable?
- We start by considering only for expressions with generators that bind simple names (no patterns)

Translating For Expressions With A Single Generator

Translating For Expressions With a Generator and a Filter

```
for (x <- expr1 if expr2) yield expr3

\mapsto

for (x <- expr1 withFilter (x => expr2)) yield expr3
```

Translating For Expressions With a Generator and a Filter

```
for (x <- expr1 if expr2) yield expr3

for (x <- expr1 withFilter (x => expr2)) yield expr3

expr1 withFilter (x => expr2) map (x => expr3)
```

For now, read this as "filter". We will return to it.

Translating For Expressions Starting With a Generator and a Filter

```
for (x <- expr1 if expr2; seq) yield expr3

Hor (x <- expr1 withFilter (x => expr2); seq)
yield expr3
```

Translating For Expressions Starting With Two Generators

```
for (x <- expr1; y <- expr2; seq) yield expr3

expr1.flatMap(x => for (y <- expr2; seq) yield expr3)</pre>
```

Translating For Expressions Example

```
for (b1 <- books; b2 <- books if b1 != b2;
    a1 <- b1.authors; a2 <- b2.authors if a1 == a2)
yield a1

books flatMap (b1 =>
    books withFilter (b2 => b1 != b2) flatMap (b2 =>
    b1.authors flatMap (a1 =>
    b2.authors withFilter (a2 => a1 == a2)
    map (a2 => a1))))
```

Translating Patterns in Generators

```
for (pat <- expr1) yield expr2

expr1 withFilter (_ match {
   case pat => true
   case _ => false
}) map (_ match {
   case pat => expr2
})
```

Other cases with patterns and for expressions are similar

Generalizing For Expressions

- Because for expressions are simply translated to expressions involving map, flatMap, and withFilter, we can use for expressions over our own collections
- We need only define: map, flatMap and withFilter
 - Because translation occurs before type checking, there is no particular type that a collection must subtype to be compatible with for-expressions

Generalizing For Expressions

- We can even define a subset of these methods and use our collection only in for expressions that translate to our subset!
 - For example, if we do not define withFilter, we cannot use our collection in a for expression with a filter

Generalizing For Expressions

- Because translation occurs before type checking, there
 is no particular signature that our methods map,
 flatMap and withFilter must satisfy!
 - All that is required is that the resulting, translated program passes type checking

- In our own List implementation, we could simply define withFilter as filter, and our collection would work with for expressions
- The idea behind withFilter is that it is often advantageous to simply wrap the collection in a view that performs the given filter on the next Map
- Because no particular type signature is required, we need only define map and flatMap on our wrapper

```
abstract class List[+T] {
    ...
    def withFilter[S >: T, U](p: S => Boolean) =
        WithFilter[S](p,this)
}
```

```
case class WithFilter[T](p: T => Boolean, xs: List[T]) {
  def map[U](f: T \Rightarrow U): List[U] = {
    xs match {
      case Empty => Empty
      case Cons(y,ys) => {
        val rest = WithFilter(p,ys) map f
        if (p(y)) Cons(f(y), rest)
        else rest
```

 Because results of withFilter are immediately taken apart by a map or a flatMap, we can still think of the result of a withFilter as being an instance of the original collection

Typical Structure of a Class That Works With For Expressions

```
abstract class C[A] {
  def map[B](f: A => B): C[B]
  def flatMap[B](f: A => C[B]): C[B]
  def withFilter(p: A => Boolean): C[A]
}
```

- In functional programming, a monad can be defined as a type for which we can formulate
 - The functions map, flatMap, and withFilter
 - A "unit constructor" which produces a monad from an element value
 - In an object-oriented language, we can think of the "unit constructor" simply as a constructor or a factory method

Because for expressions work over precisely those datatypes for which we can formulate the functions that characterize monads, we can think of for expressions as syntax for computing with monads

- But monads are able to characterize far more than just collections:
 - I/O
 - State
 - Transactions
 - Options
 - etc.

- Thus, for expressions can be used in far more general contexts than simply walking over collections
- When looking at library classes, watch for implementations of map, flatMap, withFilter
- When these functions are defined, consider expressing your computation with for expressions

Limitations of the Substitution Model of Reduction

Consider the following function definition:

```
def makeOddBooster(n: Int) = {
  require(n >= 0)
  def isEven(n: Int): Boolean = {
     (n == 0) || isOdd(n - 1)
  }
  def isOdd(n: Int): Boolean = {
   !isEven(n)
  }
  (m: Int) => if (isEven(m)) m else m + n
}
```

Limitations of the Substitution Model of Reduction

- Our makeOddBooster function cannot be expanded before it is returned
- It must remember the context in which it was formed

- Name environments map names to values
- Every expression is evaluated in the context of a name environment

• To evaluate a *name*, simply reduce to the value it is mapped to in the environment

- To evaluate a function, reduce it to a lexical closure, which consists of two parts:
 - The body of the function
 - The environment in which the body occurs

- To evaluate an application of a closure
 - Extend the environment of the closure, mapping the function's parameters to argument values
 - Evaluate the body of the closure in this new environment

Constructs that Add New Names to the Environment

- val
- def
- object
- case class
- import

- Bindings in patterns
- Function applications

Example Evaluation

```
makeOddBooster(3)(1); ENV \rightarrow
(m: Int) \Rightarrow if (isEven(m)) m else m + n)(1);
                      {n: Int = 3,}
                 isEven = Closure(...),
             isOdd = Closure(...)} ∪ ENV →
            if (isEven(m)) m else m + n;
       \{m: Int = 1, n: Int = 3, ...\} \cup ENV \rightarrow^*
              if (false) m else m + n;
       \{m: Int = 1, n: Int = 3, ...\} ∪ ENV \rightarrow
                         m + n;
       {m: Int = 1, n: Int = 3, ...} \cup ENV \mapsto
                         4; ENV
```

Takeaways

- Use Scala's for-expressions liberally
- Define map, flatMap and/or withFilter on your own monad-like data-structures to use them with for
- To evaluate non-trivial expressions, we need to keep track of an environment
- Lexical closures are used to store function values in an environment