



# Mutually Referential Data Definitions

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# Announcements and Plan

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- Homework due Thursday at 11am.
  - Why? Monday is a holiday, so we cannot hold labs on Monday.
  - Monday labs moved to Wednesday; same time and place.
- Plan for today
  - What is mutual referencing/recursion
  - Simple and deep examples illustrating the approach.



## Example of a Mutually Referential Data Definition

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```
; Descendant trees
; A parent is a structure
;   (make-parent loc n)
; where loc is a list-of-children,
;   n is a symbol

; A list-of-children is either
;   empty, or
;   (cons p loc) where
; where p is a parent, and loc is a
;   list-of-children
```



# Terminology and Template

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- Common terminology: mutually **recursive** instead of mutually **referential**
- Writing **one** function on any of these types requires writing a set of functions for **all** the mutually recursive types
- Each reference to a mutually recursive type in a **definition** corresponds to a different recursive call to the appropriate function **in** the corresponding **template**



# Template(s)

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```
; A parent is a structure
;   (make-parent n loc)
; where n is a symbol (the name of the
;   parent) and loc is a list-of-children,
(define-struct parent (name children))

; parent-fn: parent -> ...
; (define (fun-parent ... p ...)
;   (... (parent-name p) ...
;         ... (loc-fn (parent-children p)) ...))
```



# Templates, cont.

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```
; A list-of-children is either
;   empty, or
;   (cons p loc) where
; where p is a parent and loc is a list-of-children
; fun-loc: list-of-children -> ...
; (define (loc-fn ... loc ...)
;   (cond [(empty? loc) ...]
;         [else
;          ... (parent-fn ... (first loc) ...) ...
;          ... (loc-fn ... (rest loc) ...) ...]))
```



## Function calls in template(s)

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- Mutually recursive calls are part of template
  - Use of a mutually recursive type is just the same as a recursive use of a type itself
  - A set of mutually recursive type definitions is really one big recursive type definition with multiple parts and each part has a template
- The form of the function calls in the template(s) is crucial for ensuring termination



# More about termination

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- For the inductive (self-referential) types we saw before today, a recursive functions terminates if
  - it handles the base case(s) cleanly, and
  - it only make recursive calls on substructures of its primary argument, *e.g.*, the `rest` of a non-empty list
- Mutually recursive (referential) definitions are the same
  - Example: Imagine a type `box` that can contain bags, and a type `bag` that can contain boxes. Why does the template ensure termination?
    - Any box will be bigger than any bag it contains
    - Similarly for bags.
    - No infinite descending chains of containment.





# Code

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- Write a function that counts the people in a descendant tree

```
; parent-count : parent -> natural
; children-count : list-of-children -> natural
(define (parent-count p)
  (add1 (children-count (parent-children p))))
(define (children-count aloc)
  (cond [(empty? aloc) 0]
        [else (+ (parent-count (first aloc))
                  (children-count (rest aloc)))]))
```

; Note: Mutual "defines" should be contiguous



## Another Example (Unix File System)

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```
; A file is either:  
;   a rawFile, or  
;   a dir (short for directory)  
  
; A dir is a structure  
; (make-dir lonf) where lonf is a list-of-nFiles  
(define-struct dir (nFiles))  
  
; A list-of-nFiles is either:  
; ...  
  
; A nFile is a structure  
; (make-nFile name f) where name is a symbol and f is a  
  file.  
(define-struct nFile (name file))
```



# Template

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```
; A file is either:  
; a list-of-char, or  
; a dir  
  
; file-fun : f -> ...  
(define (file-fun ... f ...)  
  (cond [(rawFile? f) ...]  
        [(dir? f) ...  
         ... (dir-fun ... f ...)) ... ]))  
  
; A dir is  
;(make-dir lonf) where lonf is a list-of-nFiles  
  
; dir-fun : dir -> ...  
(define (dir-fun ... d ...)  
  ... (nFiles-fun ... (dir-nFiles d) ...) ... )
```



# Template cont.

---

```
; A list-of-nFiles is either:
; ...
(define (lonf-fun ... lonf ... )
  (cond [(empty? lonf) ... ]
        [(cons? lonf) ...
         ... (nFile-fun ... (first lonf) ... ) ... )
         ... (lonf-fun ... (rest lonf) ...) ... ]))

; A nFile is a structure
; (make-nFile name f) where name is a symbol and f is a file.
(define (nFile-fun ... nf ...)
  ... (nFile-name nf) ...
  ... (file-fun ... (nFile-file nf) ... ) ... )
```



# Example function on file system

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```
; find?: dir symbol -> boolean
; Purpose: (find? d n) determines whether a file with name n
           occurs in directory d.
; Instantiated template
#|
(define (find? d n ) ... (nFiles-find? (dir-nFiles d) n) ... )

(define (nFiles-find? lonf n)
  (cond [(empty? lonf) ...]
        [(cons? lonf)
         ... (nFile-find? (first lonf) n) ...
         ... (nFiles-find? (rest lonf) n) ... ]))

(define (nFile-find? nf n)
  ... (nFile-name nf) ...
  ... (file-find? (nFile-file nf) n) ... )
```



## Example function cont.

```
(define (find? d n) ... (nFiles-find? (dir-nFiles d) n) ... )
```

```
(define (nFiles-find? lonf n)
  (cond [(empty? lonf) ...]
        [(cons? lonf)
         ... (nFile-find? (first lonf) n) ...
         ... (nFiles-find? (rest lonf) n) ... ]))
```

```
(define (nFile-find? nf n)
  ... (nFile-name nf) ...
  ... (nFile-find? (nFile-file nf) n) ... )
```

```
(define (file-find? f n)
  (cond [(rawFile? f) ... ]
        [(dir? f) ... (find? f n) ... ]))
```

```
|#
```



# Code

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```
(define (find? d n) (nFiles-find? (dir-nFiles d) n))

(define (nFiles-find? lonf n)
  (cond [(empty? lonf) false]
        [(cons? lonf)
         (or (nFile-find? (first lonf) n)
             (nFiles-find? (rest lonf) n))]))

(define (nFile-find? nf n)
  (or (equal? (nFile-name nf) n)
      (file-find? (nFile-file nf) n)))

(define (file-find? f n)
  (cond [(rawFile? f) false]
        [(dir? f) (find? f n)]))

|#
```



## For Next Class

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- Homework deferred one day
- Labs:
  - Don't forget Tuesday lab
  - Monday labs meet Wednesday