

Comp 311

Functional Programming

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Monads

- In functional programming, a *monad* can be defined as a type for which we can formulate
 - The functions `map`, `flatMap`, and `withFilter`
 - A “unit constructor” which produces a monad from an element value
 - In an object-oriented language, we can think of the “unit constructor” simply as a constructor or a factory method

Monads

Because `for` expressions work over precisely those datatypes for which we can formulate the functions that characterize monads, we can think of `for` expressions as syntax for computing with monads

Monads

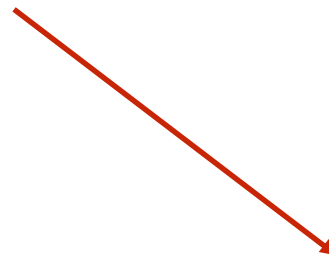
- But monads are able to characterize far more than just collections:
 - I/O
 - State
 - Transactions
 - Options
 - etc.

Monads

- Thus, `for` expressions can be used in far more general contexts than simply walking over collections
- When looking at library classes, watch for implementations of `map`, `flatMap`, `withFilter`
- When these functions are defined, consider expressing your computation with `for` expressions

Filters in For Expressions

This is a filter



```
for (x <- xs if x >= 0)  
  yield square(x) + 1
```

Filters in For Expressions

- Filters are attached to generators
- A given generator can have zero or more filters

Filters in For Expressions

```
for (  
  x <- xs  
  if x >= 0  
  if x % 2 == 0  
) yield square(x) + 1
```


Clauses Can Be Enclosed in Braces Instead of Parentheses

```
for {  
  x <- xs  
  if x >= 0  
  if x % 2 == 0  
} yield square(x) + 1
```

For Expressions Can Include Multiple Generators

```
for {  
  x <- xs  
  if x >= 0  
  y <- ys  
  if y % 2 == 0  
} yield x * y
```

For Expressions Can Include Local Bindings

```
for {  
  x <- xs  
  if x >= 0  
  square = x * x  
  y <- ys  
  if y % square == 0  
} yield x * y
```

Generators Can Specify Arbitrary Patterns

```
val xs = Cons(Square(4),  
              Cons(Circle(3),  
                  Cons(Rectangle(2,3),  
                        Empty)))
```

```
for {  
  Rectangle(x,y) <- xs  
} yield x * y
```

\mapsto^*

```
Cons(6.0, Empty)
```

Generators Can Specify Arbitrary Patterns

- Elements of the collection that do not match the pattern are filtered
- Effectively, a pattern in a `for` expression serves as part of a generator and a filter

Guidelines on Using For Expressions

- Prefer `for` expressions to maps and filters
- They tend to be easier to read:
 - All bindings and collections iterated over are listed up front
- Prefer `{...}` to `(...)` around non-trivial *for* clauses

For vs Map

- Compare:

```
for (x <- xs if x >= 0)  
  yield square(x) + 1
```

- To:

```
xs.filter(_ >= 0).map(square(_) + 1)
```

For Expressions and Database Queries

- `for` expressions are similar to standard database queries
- Consider a simple in-memory database of books, represented as a list of `Book` instances (*Odersky et al 2012*):

```
case class Book(title: String, authors: String*)
```


For Expressions and Database Queries

```
val books: List[Book] =  
  Cons(  
    Book(  
      "Structure and Interpretation of Computer Programs",  
      "Abelson, Harold", "Sussman, Gerald J."  
    ),  
    Book(  
      "How to Design Programs",  
      "Felleisen, Matthias", "Findler, Robert Bruce",  
      "Flatt, Mathew", "Krishnamurthi, Shriram"  
    ),  
    Book(  
      "Programming in Scala",  
      "Odersky, Martin", "Spoon, Lex", "Venners, Bill"  
    )  
  )  
  ...  
)
```

Finding All Books Whose Author Has Last Name “Sussman”

```
for {  
  b <- books  
  a <- b.authors  
  if a startsWith “Sussman,”  
} yield b.title
```

Finding All Books That Have The String “Program” In the Title

```
for {  
  b <- books  
  if b.title indexOf “Program” >= 0  
} yield b.title
```

Finding All Authors That Have Written More Than One Book in the Database

```
for {  
  b1 <- books  
  b2 <- books if b1 != b2  
  a1 <- b1.authors  
  a2 <- b2.authors  
  if a1 == a2  
} yield a1
```

Translating For Expressions

- For expressions are simply translated to maps, flatMaps, and filters by the Scala compiler
- Translation occurs *before* type checking
 - Why is this preferable?
- We start by considering only for expressions with generators that bind simple names (no patterns)

Translating For Expressions With A Single Generator

```
for (x <- expr1) yield expr2  
  ↪  
expr1.map(x => expr2)
```

Translating For Expressions With a Generator and a Filter

```
for (x <- expr1 if expr2) yield expr3
```

↪

```
for (x <- expr1 withFilter (x => expr2)) yield expr3
```

Translating For Expressions With a Generator and a Filter

```
for (x <- expr1 if expr2) yield expr3
  ↪
for (x <- expr1 withFilter (x => expr2)) yield expr3
  ↪
expr1 withFilter (x => expr2) map (x => expr3)
```

For now, read this as “filter”. We will return to it.

Translating For Expressions

Starting With a Generator and a Filter

```
for (x <- expr1 if expr2; seq) yield expr3
```

↳

```
for (x <- expr1 withFilter (x => expr2); seq)  
  yield expr3
```

Translating For Expressions Starting With Two Generators

```
for (x <- expr1; y <- expr2; seq) yield expr3
```

↳

```
expr1.flatMap(x => for (y <- expr2; seq) yield expr3)
```

Translating For Expressions

Example

```
for (b1 <- books; b2 <- books if b1 != b2;  
     a1 <- b1.authors; a2 <- b2.authors if a1 == a2)  
yield a1
```

↪

```
books flatMap (b1 =>  
  books withFilter (b2 => b1 != b2) flatMap (b2 =>  
    b1.authors flatMap (a1 =>  
      b2.authors withFilter (a2 => a1 == a2)  
      map (a2 => a1))))
```

Translating Patterns in Generators

```
for (pat <- expr1) yield expr2  
↳  
expr1 withFilter ( _ match {  
  case pat => true  
  case _ => false  
}) map ( _ match {  
  case pat => expr2  
})
```

Other cases with patterns and for
expressions are similar

Generalizing For Expressions

- Because for expressions are simply translated to expressions involving `map`, `flatMap`, and `withFilter`, we can use for expressions over our own collections
- We need only define: `map`, `flatMap` and `withFilter`
 - Because translation occurs before type checking, there is no particular type that a collection must subtype to be compatible with for-expressions

Generalizing For Expressions

- We can even define a subset of these methods and use our collection only in for expressions that translate to our subset!
- For example, if we do not define `withFilter`, we cannot use our collection in a for expression with a filter

Generalizing For Expressions

- Because translation occurs before type checking, there is no particular signature that our methods `map`, `flatMap` and `withFilter` must satisfy!
- All that is required is that the resulting, translated program passes type checking

Typical Structure of a Class That Works With For Expressions

```
abstract class C[A] {  
  def map[B](f: A => B): C[B]  
  def flatMap[B](f: A => C[B]): C[B]  
  def withFilter(p: A => Boolean): C[A]  
}
```


Takeaways

- Use Scala's *for-expressions* liberally
- Define `map`, `flatMap` and/or `withFilter` on your own monad-like data-structures to use them with *for*