COMP 322: Fundamentals of Parallel Programming

Lecture 21: Linearizability of Concurrent Objects

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Announcements

- Graded midterm exams can be picked up from Amanda Nokleby in Duncan Hall room 3137
- Homework 5 (written assignment) has been posted
 Deadline: 5pm on Friday, March 18th
- Homework 6 (HJ programming assignment) will be given on March 18th
- Homework 7 (Concurrent Java programming assignment) will be given on April 1st (really!)



Acknowledgments for Today's Lecture

- Lecture 21 handout
- Maurice Herlihy and Nir Shavit. The art of multiprocessor programming. Morgan Kaufmann, 2008.
 - -Optional text for COMP 322
 - —Slides and code examples extracted from <u>http://www.elsevierdirect.com/companion.jsp?ISBN=9780123705914</u>



Concurrent Objects

- A concurrent object is an object that can correctly handle methods invoked in parallel by different tasks or threads
 - -Originally referred to as monitors
 - -Also informally referred to as "thread-safe objects"
- For simplicity, it is usually assumed that the body of each method in a concurrent object is itself sequential

-Assume that method does not create child async tasks

- Implementations of methods can be serial (e.g., enclose each method in an isolated statement like a critical section) or concurrent (e.g., ConcurrentHashMap, ConcurrentLinkedQueue and CopyOnWriteArraySet)
- A desirable goal is to develop method implementations that are concurrent while being as close to the semantics of the serial version as possible

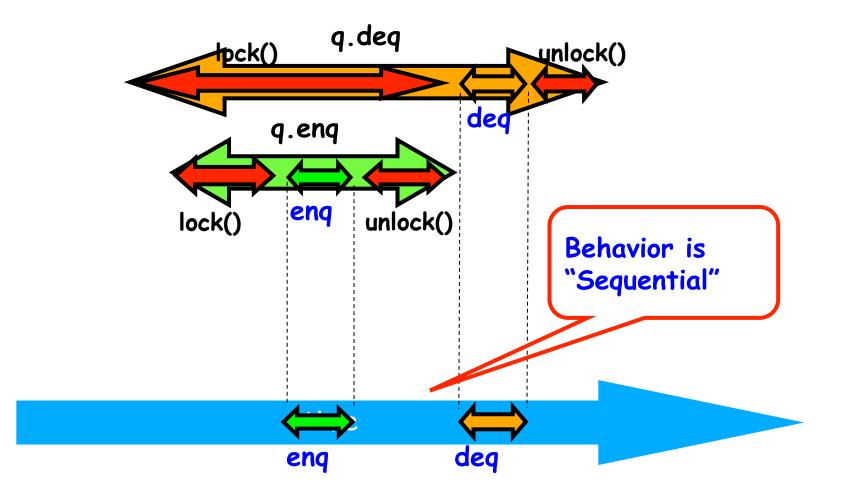


The Big Question!

- Consider a simple FIFO (First In, First Out) queue as a canonical example of a concurrent object
 - -Method q.enq(o) inserts object o at the tail of the queue
 - Assume that there is unbounded space available for all enq() operations to succeed
 - -Method q.deq() removes and returns the item at the head of the queue.
 - Throws EmptyException if the queue is empty.
- What does it mean for a *concurrent* object like a FIFO queue to be correct?
 - -What is a concurrent FIFO queue?
 - -FIFO means strict temporal order
 - -Concurrent means ambiguous temporal order



Describing the concurrent via the sequential



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Informal definition of Linearizability

- **1**. A linearizable execution is one in which the semantics of a set of method calls performed in parallel on a concurrent object is equivalent to that of some legal linear sequence of those method calls.
- **2.** A *linearizable concurrent object* is one for which all possible executions are linearizable.



Table 1: Example execution of a monitorbased implementation of FIFO queue q

Is this a linearizable execution?

Time	Task A	Task B
0	Invoke q.enq(x)	
1	Work on q.enq(x)	
2 $ $	Work on q.enq(x)	
3	Return from q.enq(x)	
4		Invoke q.enq(y)
5		Work on q.enq(y)
6		Work on q.enq(y)
7		Return from q.enq(y)
8		Invoke q.deq()
9		Return x from q.deq()

Yes! Equivalent to "q.enq(x) ; q.enq(y) ; q.deq():x"



Table 2: Example execution of method calls on a concurrent FIFO queue q

Is this a linearizable execution?

Time	Task A	Task B
0	Invoke q.enq(x)	
1	Work on q.enq(x)	Invoke q.enq(y)
$\begin{vmatrix} 2 \end{vmatrix}$	Work on q.enq(x)	Return from q.enq(y)
3	Return from q.enq(x)	
4		Invoke q.deq()
5		Return x from q.deq()

Yes! Equivalent to "q.enq(x) ; q.enq(y) ; q.deq():x"

 Would the execution be linearizable if q.deq() returned y instead of x?



Table 3: Example of a non-linearizable execution on a concurrent FIFO queue q

Is this a linearizable execution?

Time	Task A	Task B
0	Invoke q.enq(x)	
1	Return from q.enq(x)	
2		Invoke q.enq(y)
3	Invoke q.deq()	Work on q.enq(y)
4	Work on q.deq()	Return from q.enq(y)
5	Return y from q.deq()	

 No! q.enq(x) must precede q.enq(y) in all linear sequences of method calls invoked on q. It is illegal for the q.deq() operation to return y.



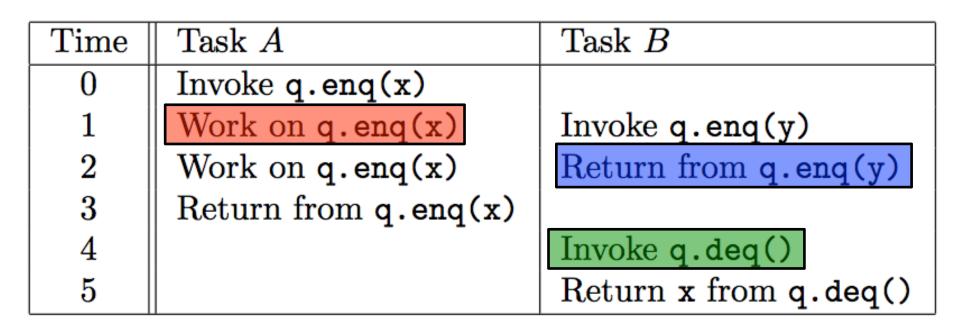
Alternate definition of Linearizability

- Assume that each method call takes effect "instantaneously" at some distinct point in time between its invocation and return.
- Execution is linearizable if we can choose instantaneous points that are consistent with a sequential execution in which methods are executed at those points



Table 2: Example execution of method calls on a concurrent FIFO queue q

Is this a linearizable execution?

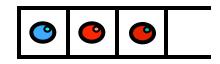


Yes! Equivalent to "q.enq(x) ; q.enq(y) ; q.deq():x"

 Would the execution be linearizable if q.deq() returned y instead of x?

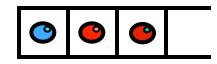


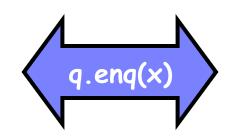
An Example







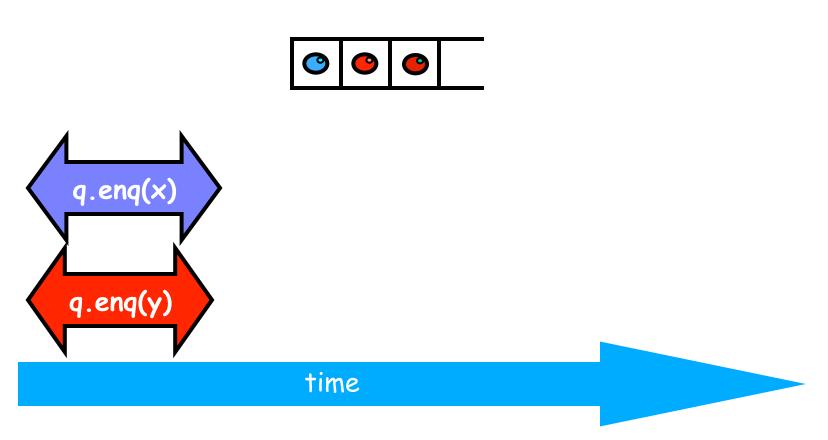






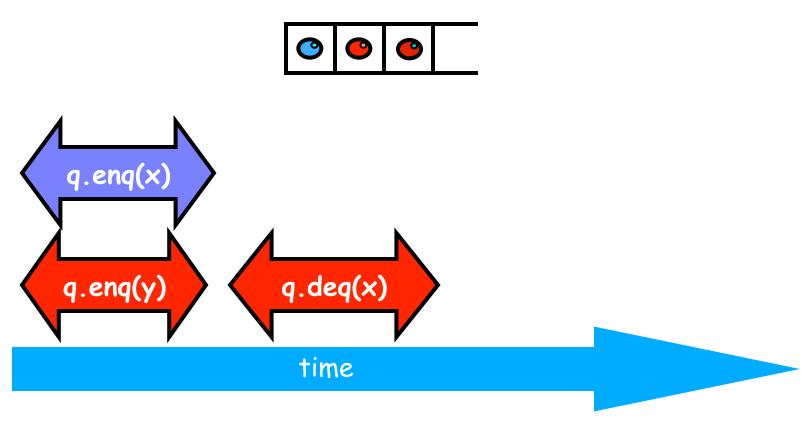
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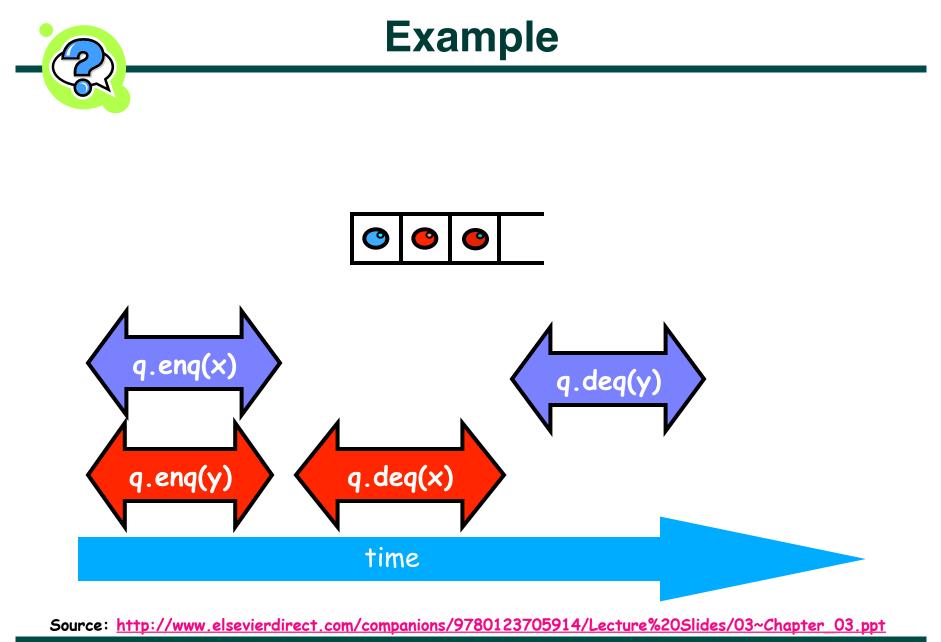




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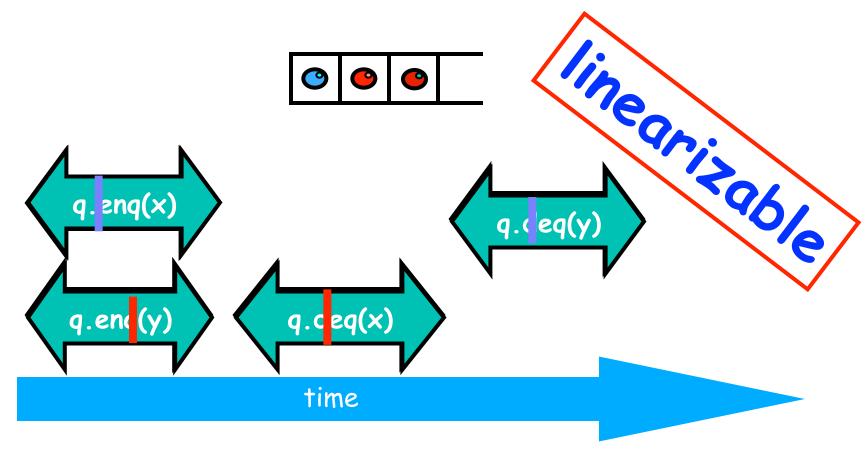






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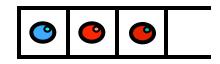




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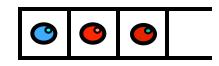
Another Example (like Table 3)

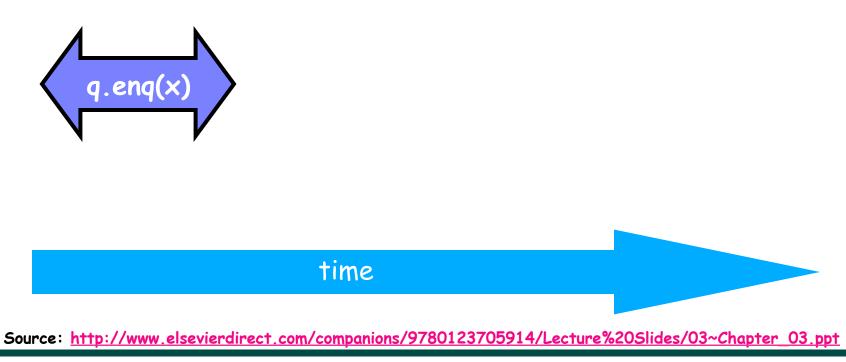






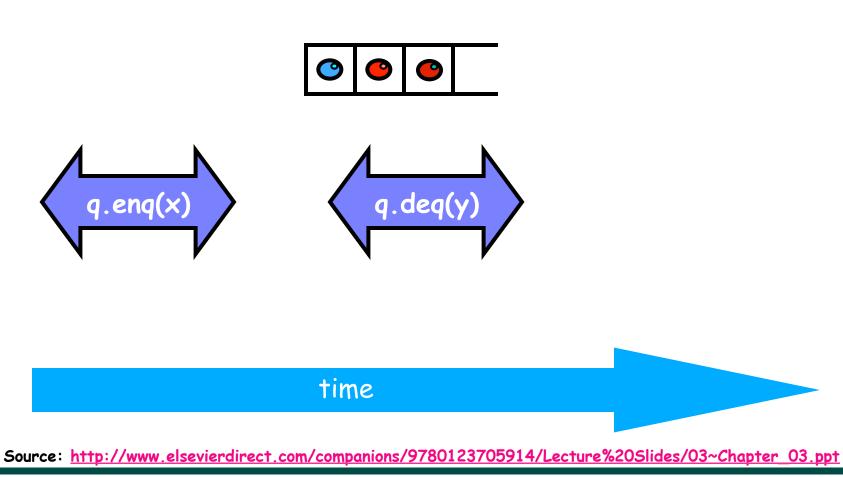
Another Example





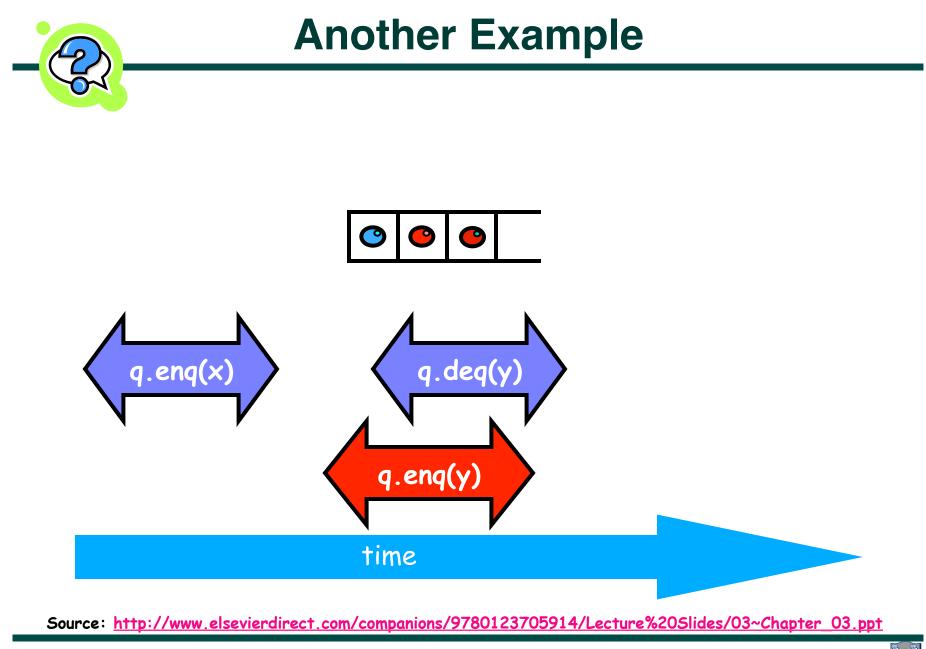


Another Example



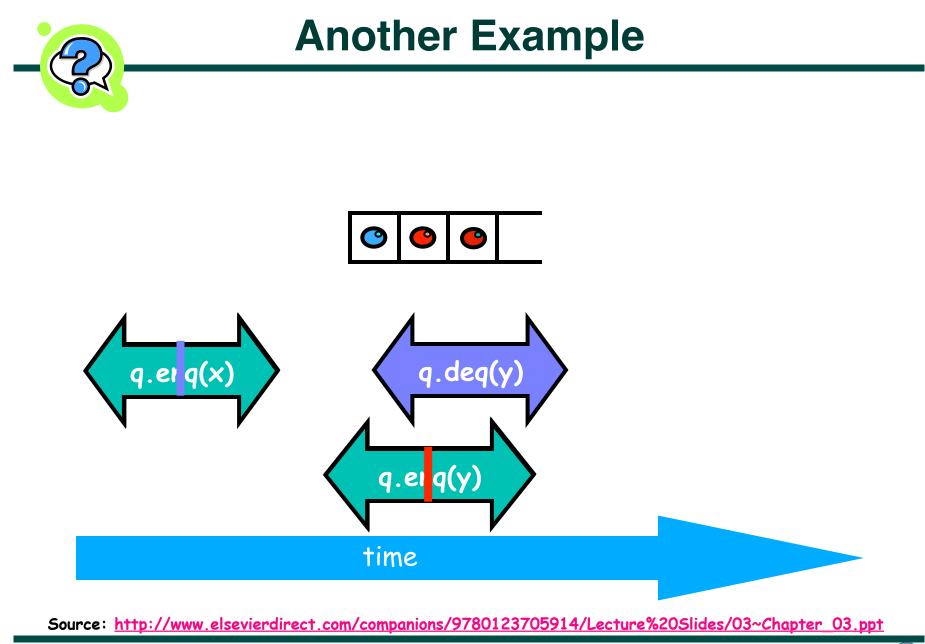






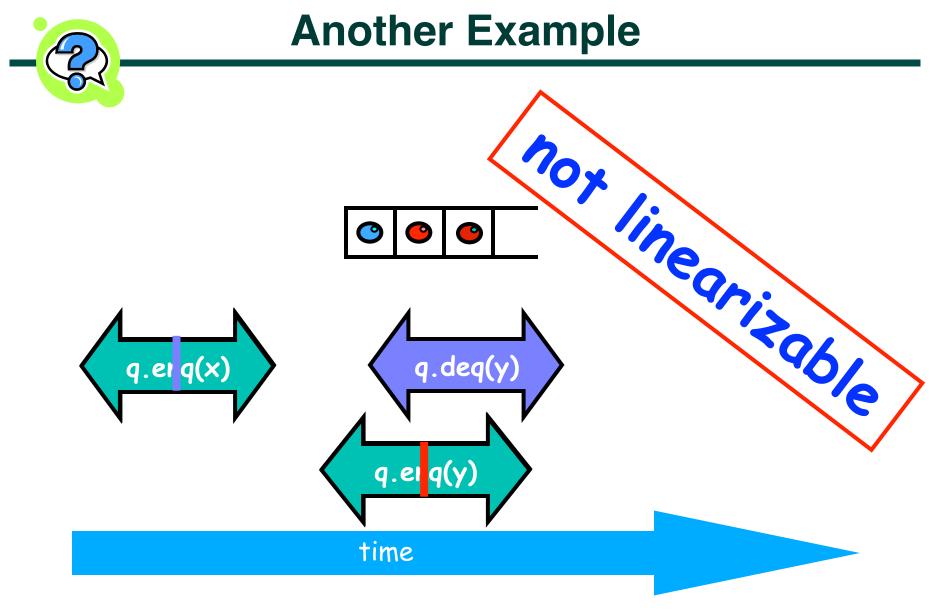
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Figure 1: Computation Graph for monitorbased implementation of FIFO queue (Table 1)

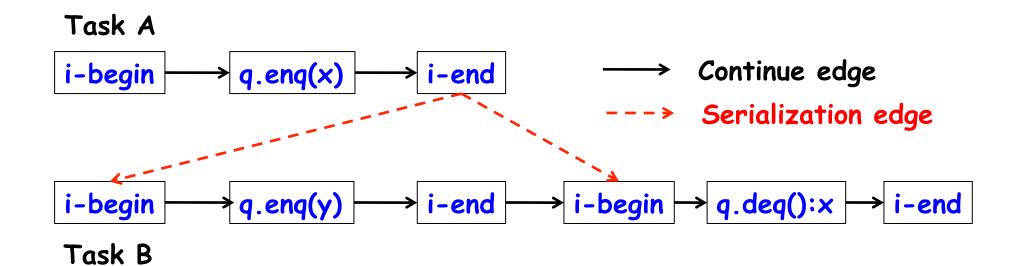
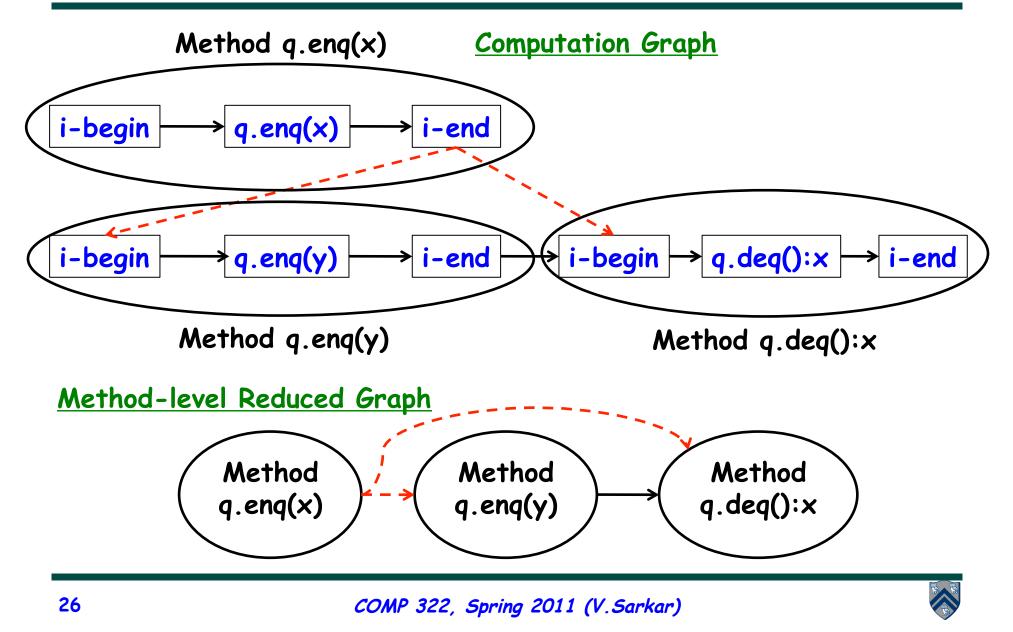




Figure 2: Creating a Reduced Graph to model Instantaneous Execution of Methods



Relating Linearizability to the Computation Graph model

- Given a reduced CG, a sufficient condition for linearizability is that the reduced CG is acyclic as in Figure 2.
- This means that if the reduced CG is acyclic, then the underlying execution must be linearizable.
- However, the converse is not necessarily true, as we will see.



Figure 3: example Computation Graph for concurrent implementation of FIFO queue (Table 2)

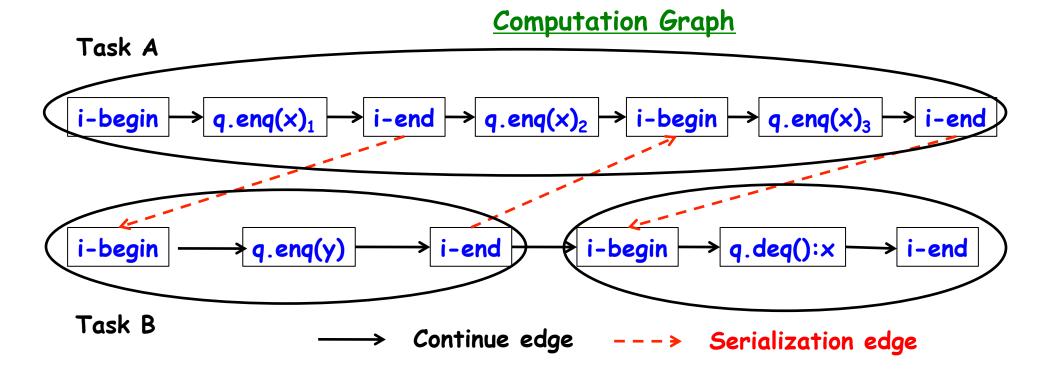
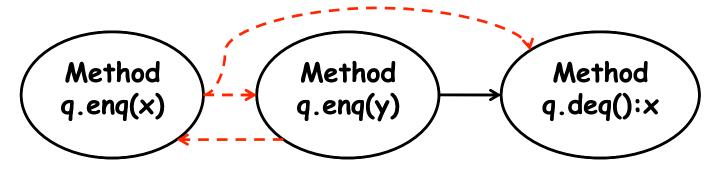




Figure 4: Reduced method-level graph for Computation Graph in Figure 3

• Example of linearizable execution graph for which reduced method-level graph is cyclic



- Approach to make cycle test more precise for linearizability
 - Decompose concurrent object method into a sequence of "try" steps followed by a sequence of "commit" steps
 - Assume that each "commit" step's execution does not use any input from any prior "try" step
 - ➔ Reduced graph can just reduce each "commit" step to a single node instead of reducing entire method into a single node

