COMP 322: Fundamentals of Parallel Programming

Lecture 3: Computation Graphs, Abstract Performance Metrics

Vivek Sarkar Department of Computer Science, Rice University <u>vsarkar@rice.edu</u>

https://wiki.rice.edu/confluence/display/PARPROG/COMP322





Announcements

- Coursera forum on HJ Environment and Setup Issues
 - Please post your issues, and also respond to postings by other students when you can help
- Instructor's office hours are during 2pm 3pm on MWF
 - Please stop by if you have problems with any of the following
 - Accessing the Module 1 handout
 - Using the turnin script
 - You did not receive any email sent to comp322-all
- Homework 1 has been posted
 - Contains written and programming components
 - Due by 5pm on Wednesday, Jan 23rd
 - Must be submitted using "turnin" script introduced in Lab 1
 - In case of problems, email a zip file to comp322-staff at mailman.rice.edu before the deadline
 - See course web site for penalties for late submissions



Complexity Measures for Computation Graphs (Recap)

Define

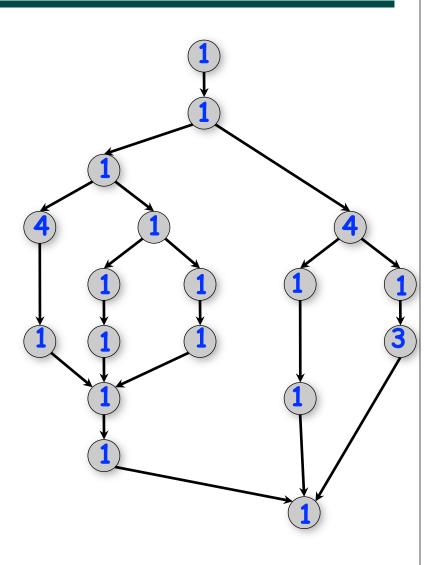
- TIME(N) = execution time of node N
- WORK(G) = sum of TIME(N), for all nodes N in CG G
 -WORK(G) is the total work to be performed in G
- CPL(G) = length of a longest path in CG G, when adding up execution times of all nodes in the path
 - -Such paths are called critical paths
 - -CPL(G) is the length of these paths (critical path length)
 - -CPL(G) is also the smallest possible execution time for the computation graph



Ideal Parallelism (Recap)

Define ideal parallelism of Computation Graph G as the ratio, WORK(G)/CPL(G)

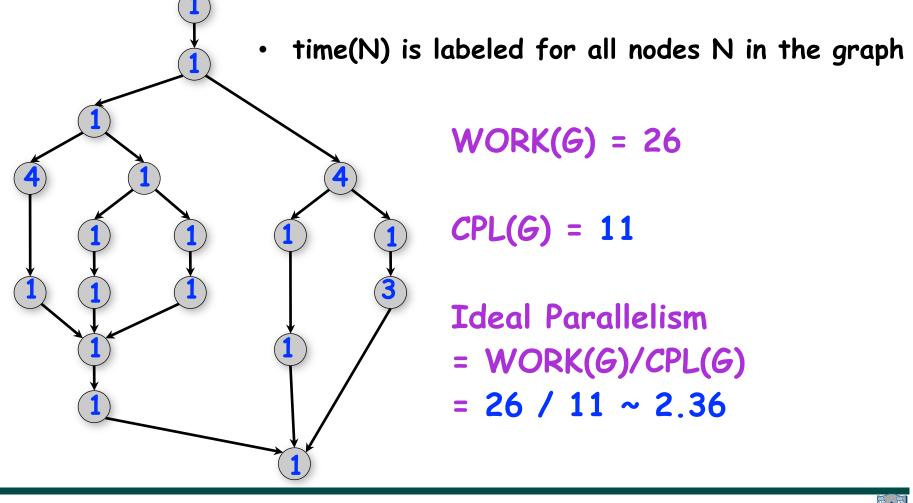
Ideal Parallelism is independent of the number of processors that the program executes on, and only depends on the computation graph





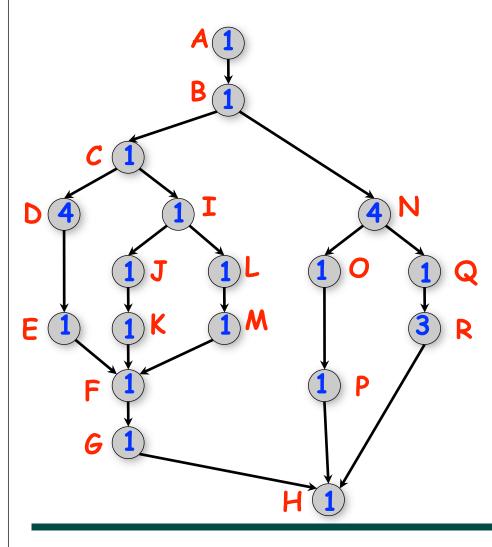
Solution to Worksheet #2: what is the critical path length and ideal parallelism of this graph?

CPL(G) = length of a longest path in computation graph G





Scheduling of a Computation Graph on a fixed number of processors: Example



6

Start time	Proc 1	Proc 2	Proc 3
0	A		
1	В		
2	С	N	
3	D	Ν	I
4	D	Ν	J
5	D	Ν	K
6	D	Q	L
7	Е	R	M
8	F	R	0
9	G	R	Ρ
10	н		
11			





Scheduling of a Computation Graph on a fixed number of processors, P

- Assume that node N takes TIME(N) regardless of which processor it executes on, and that there is no overhead for creating parallel tasks
- A schedule specifies the following for each node

-START(N) = start time

-PROC(N) = index of processor in range 1...P

```
such that
```

- —START(i) + TIME(i) <= START(j), for all CG edges from i
 to j (Precedence constraint)</pre>
- -A node occupies consecutive time slots in a processor (Nonpreemption constraint)
- -All nodes assigned to the same processor occupy distinct time slots (Resource constraint)



Lower Bounds on Execution Time of Schedules

- Let T_P = execution time of a schedule for computation graph G on P processors
 —Can be different for different schedules
- Lower bounds for all greedy schedules

 —Capacity bound: T_P ≥ WORK(G)/P
 —Critical path bound: T_P ≥ CPL(G)
- Putting them together

 −T_P ≥ max(WORK(G)/P, CPL(G))



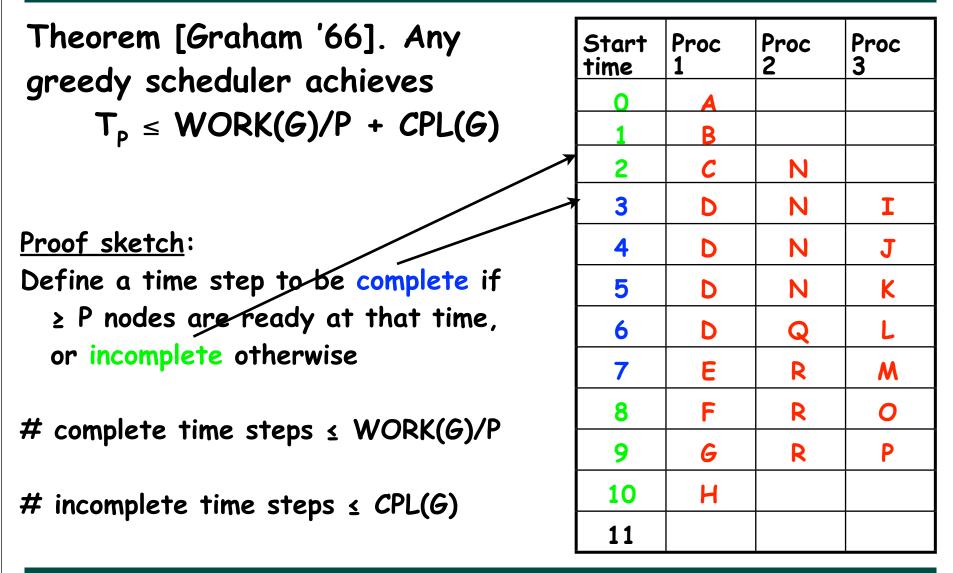
Greedy Schedule

• A greedy schedule is one that never forces a processor to be idle when one or more nodes are ready for execution

- A node is ready for execution if all its predecessors have been executed
- Observations
 - $-T_1 = WORK(G)$, for all greedy schedules
 - $-T_{\infty} = CPL(G)$, for all greedy schedules

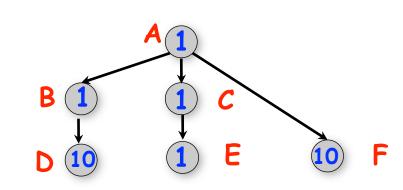


Upper Bound on Execution Time of Greedy Schedules





What are the best-case and worst-case schedules that we can obtain for this example on 2 processors?



- •WORK(G) = 24
- •CPL(G) = 12
- •For P=2, WORK(G)/P = 12
- •Lower bound = max(12, 12) = 12
- •Upper bound = 12 + 12 = 24

for T_2 are in the range, 12 ... 24

Best case, T ₂ = 13 Worst case							
Start time	Proc 1	Proc 2		Start time	Proc		
0	A			0	A		
1	В	F		1	F		
2	D	F		2	F		
3	D	F		3	F		
4	D	F		4	F		
5	D	F		5	F		
6	D	F		6	F		
7	D	F		7	F		
8	D	F		8	F		
9	D	F		9	F		
10	D	F		10	F		
11	D	С		11			
12		Е		12			
13				13			
				14			



= 14

Proc 2

В

С

Ε

D

D

D

D

D

D

D

D

D

D

1

Bounding the performance of Greedy Schedulers

Combine lower and upper bounds to get

 $max(WORK(G)/P, CPL(G)) \leq T_{P} \leq WORK(G)/P + CPL(G)$

Corollary 1: Any greedy scheduler achieves execution time T_p that is within a factor of 2 of the optimal time (since max(a,b) and (a+b) are within a factor of 2 of each other, for any $a \ge 0, b \ge 0$).

Corollary 2: Lower and upper bounds approach the same value whenever

- There's lots of parallelism, WORK(G)/CPL(G) >> P
- Or there's little parallelism, WORK(G)/CPL(G) << P

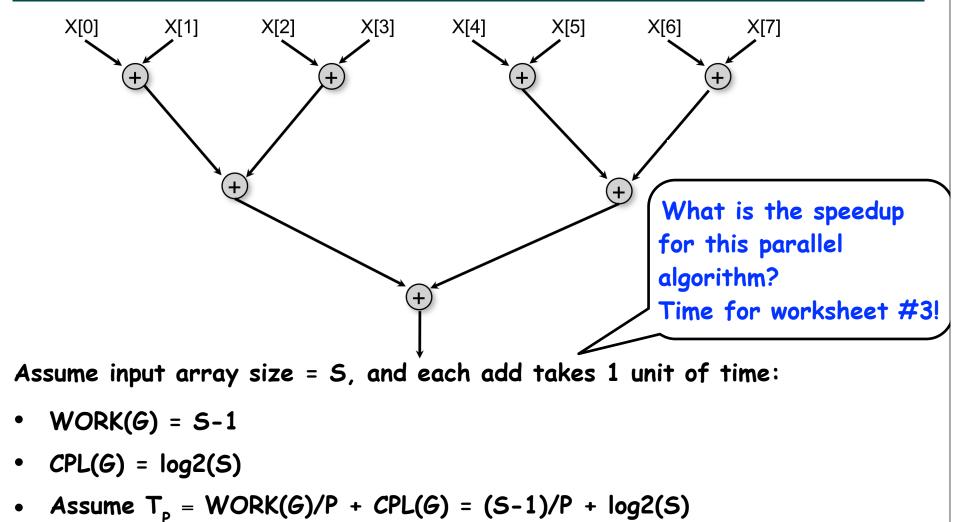


Strong Scaling and Speedup

- Define Speedup(P) = T_1 / T_P
 - -Factor by which the use of P processors speeds up execution time relative to 1 processor, for a fixed input size
 - —For ideal executions without overhead, 1 <= Speedup(P) <= P</p>
 - -Linear speedup
 - When Speedup(P) = k*P, for some constant k,
 0 < k < 1
- Referred to as "strong scaling" because input size is fixed



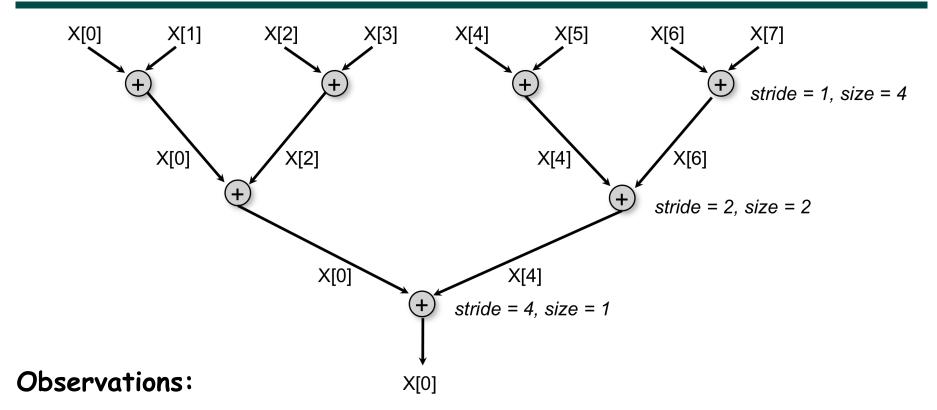
Reduction Tree Schema for computing Array Sum in parallel



• Within a factor of 2 of any schedule's execution time



Algorithm based on updates to array



- This algorithm overwrites X (make a copy if X is needed later)
- stride = distance between array subscript inputs for each addition
- size = number of additions that can be executed in parallel in each level (stage)



Async-Finish Parallel Program for Array Sum (for X.length = 8)

```
1.finish { //STAGE 1: stride = 1, size = 4 parallel additions
   async X[0] + = X[1]; async X[2] + = X[3];
2.
   async X[4]+=X[5]; async X[6]+=X[7];
3.
4.}
5.finish { //STAGE 2: stride = 2, size = 2 parallel additions
   async X[0] += X[2]; async X[4] += X[6];
6.
7.}
8.finish { //STAGE 3: stride = 4, size = 1 parallel additions
9. async X[0]+=X[4];
10.}
11.// Final sum is now in X[0]
```

Generalization to arbitrary sized arrays (ArraySum1)

```
1.for ( int stride = 1; stride < X.length ; stride *= 2 ) {
```

- 2. // Compute size = number of adds to be performed in stride
- 3. int size=ceilDiv(X.length,2*stride);
- 4. finish for(int i = 0; i < size; i++)

```
5. async {
```

6. if ((2*i+1)*stride < X.length)

```
7. X[2*i*stride] += X[(2*i+1)*stride];
```

```
8. } // finish-for-async
```

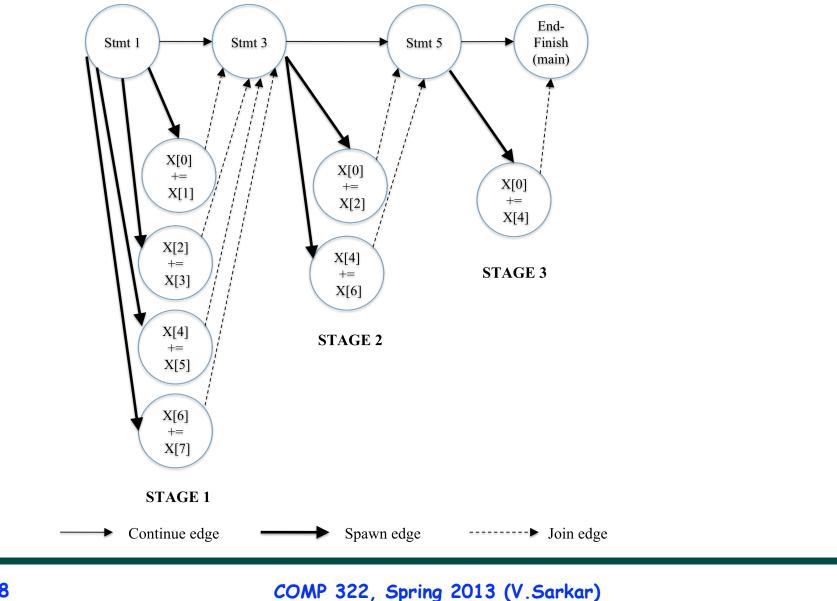
9.} // for

10.

```
11.// Divide x by y, and round up to next largest int
12.static int ceilDiv(int x, int y) { return (x+y-1) / y; }
```



Computation Graph for ArraySum1







HJ Abstract Performance Metrics

- Basic Idea
 - -Count operations of interest, as in big-O analysis
 - -Abstraction ignores overheads that occur on real systems
- Calls to perf.doWork()
 - —Programmer inserts calls of the form, perf.doWork(N), within a step to indicate abstraction execution of N application-specific abstract operations
 - e.g., adds, compares, stencil ops, data structure ops
 - -Multiple calls add to the execution time of the step
- Enabled by selecting "Show Abstract Execution Metrics" in DrHJ compiler options (or -perf=true runtime option)
 - —If an HJ program is executed with this option, abstract metrics are printed at end of program execution with WORK(G), CPL(G), Ideal Speedup = WORK(G)/ CPL(G)





Inserting call to perf.doWork() in ArraySum1

```
1.for ( int stride = 1; stride < X.length ; stride *= 2 ) {
```

- 2. // Compute size = number of adds to be performed in stride
- 3. int size=ceilDiv(X.length,2*stride);

```
4. finish for(int i = 0; i < size; i++)
```

```
5. async {
```

}

```
6. if ( (2*i+1)*stride < X.length ) {
```

```
7. perf.doWork(1);
```

```
8. X[2*i*stride] += X[(2*i+1)*stride];
```

```
9.
```

```
10. } // finish-for-async
```

11.} // for

12.



