COMP 322: Fundamentals of Parallel Programming

Lecture 3: Multiprocessor Scheduling

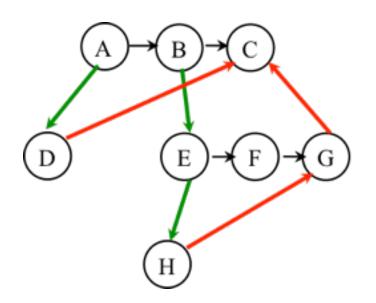
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COMP 322 January 2019 Lecture 3



One Possible Solution to Worksheet 2 (Reverse Engineering a Computation Graph)



Observations:

- Any node with out-degree > 1 must be an async (must have an outgoing spawn edge)
- Any node with in-degree > 1 must be an endfinish (must have an incoming join edge
- Adding or removing transitive edges does not impact ordering constraints

- 1.A();
- 2.finish { // F1
- 3. async D();
- 4. B();
- 5. E();
- 6. finish { // F2
- 7. async H();
- 8. F();
- 9. } // F2
 - 10. G();
- 11.} // F1
- 12.C();



Ordering Constraints and Transitive Edges in a Computation Graph

- The primary purpose of a computation graph is to determine if an ordering constraint exists between two steps (nodes)
 - -Observation: Node A must be performed before node B if there is a path of directed edges from A and B

- An edge, X → Y, in a computation graph is said to be *transitive* if there exists a path of directed edges from X to Y that does not include the X → Y edge
 - -Observation: Adding or removing a transitive edge does not change the ordering constraints in a computation graph



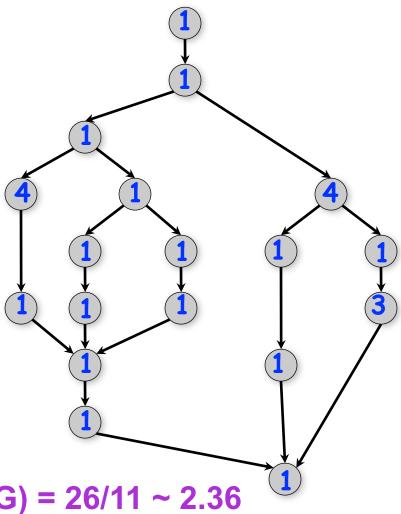
Ideal Parallelism (Recap)

- Define ideal parallelism of Computation Graph G as the ratio, WORK(G)/CPL(G)
- Ideal Parallelism only depends on the computation graph, and is the speedup that you can obtain with an unbounded number of processors

Example:

- WORK(G) = 26
- **CPL(G) = 11**

Ideal Parallelism = WORK(G)/CPL(G) = 26/11 ~ 2.36





What is the critical path length of this parallel computation?

- 1. finish { // F1
- 2. async A; // Boil water & pasta (10)
- 3. finish { // F2
- 4. async B1; // Chop veggies (5)
- 5. async B2; // Brown meat (10)
- 6. } // F2
- 7. B3; // Make pasta sauce (5)
- 8. } // F1

Step A



Step B1





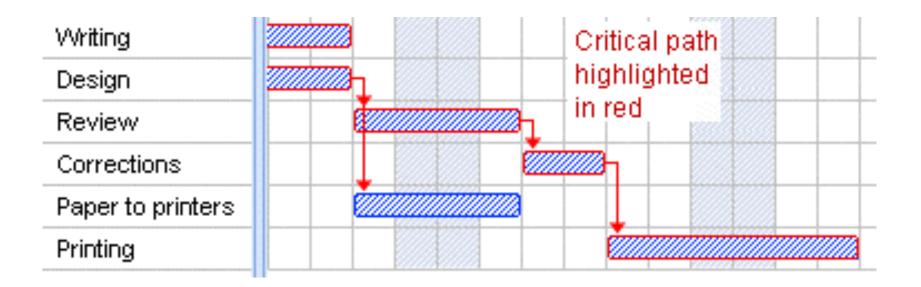


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Computation Graphs are used in Project Scheduling as well

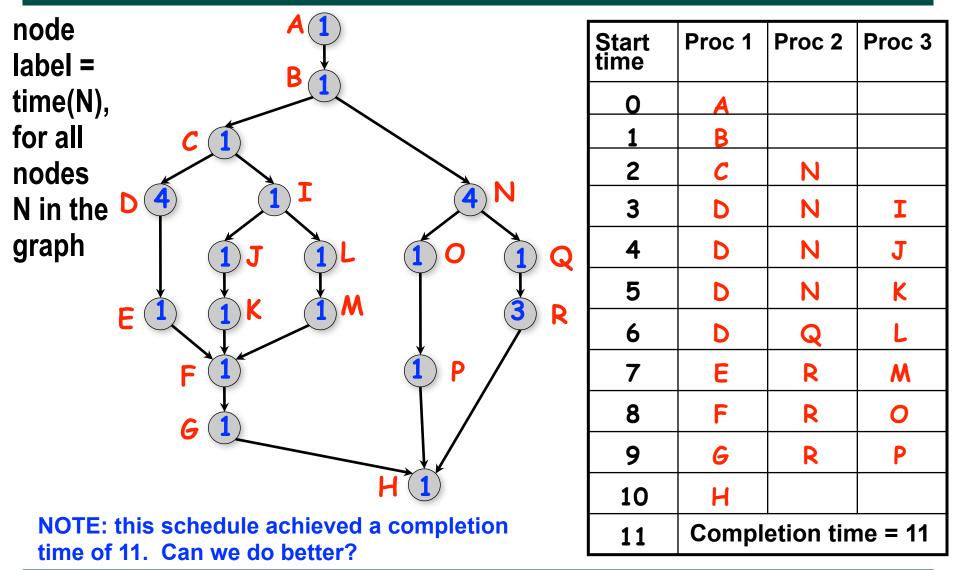
- Computation graphs are referred to as "Gantt charts" in project management
- Sample project for preparing a printed document

-Source: http://www.gantt.com/creating-gantt-charts.htm





Scheduling of a Computation Graph on a fixed number of processors: Example





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Scheduling of a Computation Graph on a fixed number of processors, P

- Assume that node N takes TIME(N) regardless of which processor it executes on, and that there is no overhead for creating parallel tasks
- A schedule specifies the following for each node

—START(N) = start time

—PROC(N) = index of processor in range 1...P

such that

—START(i) + TIME(i) <= START(j), for all CG edges from i to j
(Precedence constraint)</pre>

—A node occupies consecutive time slots in a processor (Nonpreemption constraint)

—All nodes assigned to the same processor occupy distinct time slots (Resource constraint)



Greedy Schedule

- A greedy schedule is one that never forces a processor to be idle when one or more nodes are ready for execution
- A node is ready for execution if all its predecessors have been executed
- Observations

__T₁ = WORK(G), for all greedy schedules

 $-T_{\infty}$ = CPL(G), for all greedy schedules

 where T_P(S) = execution time of schedule S for computation graph G on P processors



Lower Bounds on Execution Time of Schedules

- Let T_P = execution time of a schedule for computation graph G on P processors
 —T_P can be different for different schedules, for same values of G and P
- Lower bounds for all greedy schedules —Capacity bound: T_P ≥ WORK(G)/P

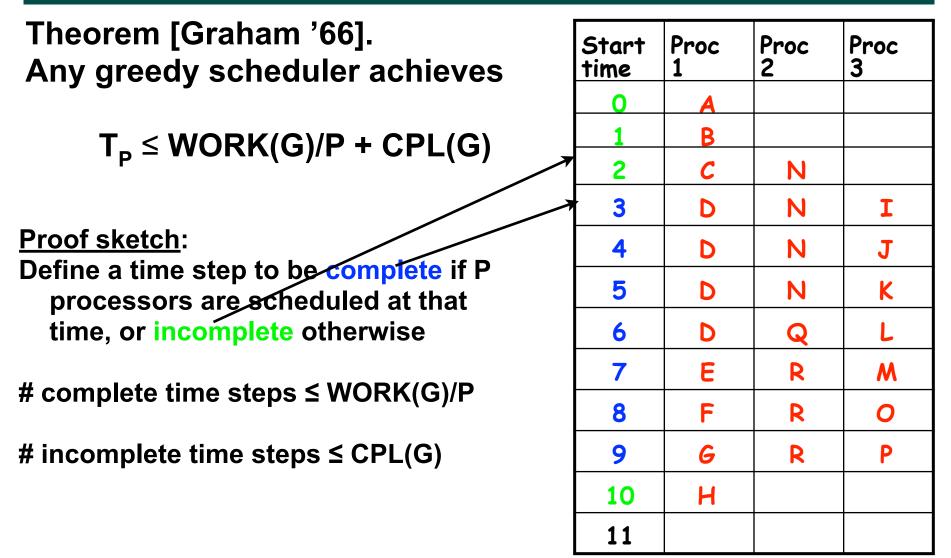
—Critical path bound: $T_P \ge CPL(G)$

• Putting them together

 $-T_{P} \ge max(WORK(G)/P, CPL(G))$



Upper Bound on Execution Time of Greedy Schedules





Bounding the performance of Greedy Schedulers

Combine lower and upper bounds to get

 $max(WORK(G)/P, CPL(G)) \le T_P \le WORK(G)/P + CPL(G)$

Corollary 1: Any greedy scheduler achieves execution time T_P that is within a factor of 2 of the optimal time (since max(a,b) and (a+b) are within a factor of 2 of each other, for any $a \ge 0$, $b \ge 0$).

Corollary 2: Lower and upper bounds approach the same value whenever

- There's lots of parallelism, WORK(G)/CPL(G) >> P
- Or there's little parallelism, WORK(G)/CPL(G) << P



Abstract Performance Metrics (Lab 1)

- Basic Idea
 - Count operations of interest, as in big-O analysis, to evaluate parallel algorithms
 - Abstraction ignores many overheads that occur on real systems
- Calls to doWork()
 - Programmer inserts calls of the form, doWork(N), within a step to indicate abstraction execution of N application-specific abstract operation
 - e.g., in the Homework 1 programming assignment (Parallel Sort), we will include one call to doWork(1) in each call to compareTo(), and ignore the cost of everything else
- Abstract metrics are enabled by calling HjSystemProperty.abstractMetrics.set(true) at start of program execution
- If an HJ program is executed with this option, abstract metrics can be printed at end of program execution with calls to abstractMetrics().totalWork(), abstractMetrics().criticalPathLength(), and abstractMetrics().idealParallelism()



Announcements & Reminders

• IMPORTANT:

-Watch video & read handout for topic 1.5 for next lecture on Monday, Jan 14th

- HW1 was posted on the course web site (<u>http://comp322.rice.edu</u>) on Jan 9th, and is due on Wednesday, Jan 23rd
- See course web site for all work assignments and due dates
- See <u>Office Hours</u> link on course web site for latest office hours schedule.

