



COMP 322: Fundamentals of Parallel Programming

Lecture 29: Linearizability

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Lecture 29



Linearizability: Correctness of Concurrent Objects

• A concurrent object is an object that can correctly handle methods invoked concurrently by different tasks or threads

-e.g., AtomicInteger, ConcurrentHashMap, ConcurrentLinkedQueue, ...

• For the discussion of linearizability, we will assume that the body of each method in a concurrent object is itself sequential

—Assume that methods do not create threads or async tasks





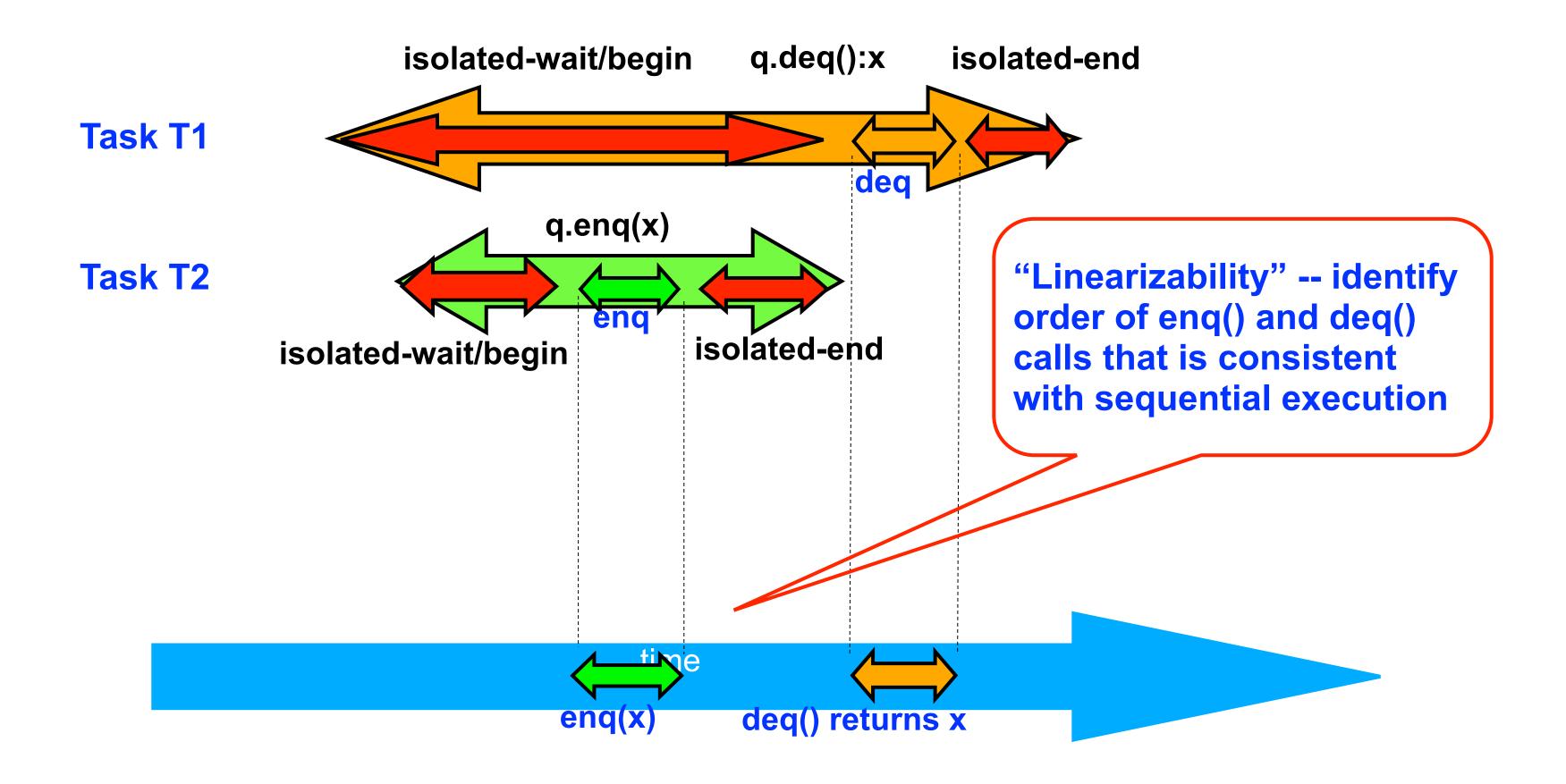
Linearizability: Correctness of Concurrent Objects

- Consider a simple FIFO (First In, First Out) queue as a canonical example of a concurrent object —Method q.enq(o) inserts object o at the tail of the queue - Assume that there is unbounded space available for all enq() operations to succeed —Method q.deq() removes and returns the item at the head of the queue. Throws EmptyException if the queue is empty.
- deq() is correct or not, in a sequential program
- How can we tell if the execution is correct for a parallel program?

• Without seeing the implementation of the FIFO queue, we can tell if an execution of calls to enq() and



Linearization: Identifying a sequential order of concurrent method calls



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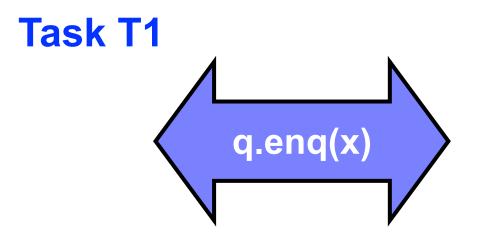
- and return.
- with a sequential execution in which methods are executed at those points
 - It's okay if some other set of instantaneous points is not linearizable
- A concurrent object is linearizable if all its executions are linearizable
 - Linearizability is a "black box" test based on the object's behavior, not its internals

Informal Definition of Linearizability

• Assume that each method call takes effect "instantaneously" at some point in time between its invocation

• An execution (schedule) is linearizable if we can choose one set of instantaneous points that is consistent

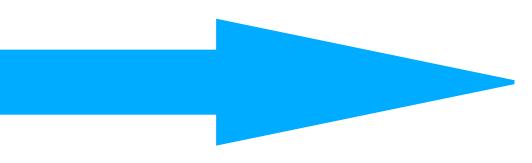






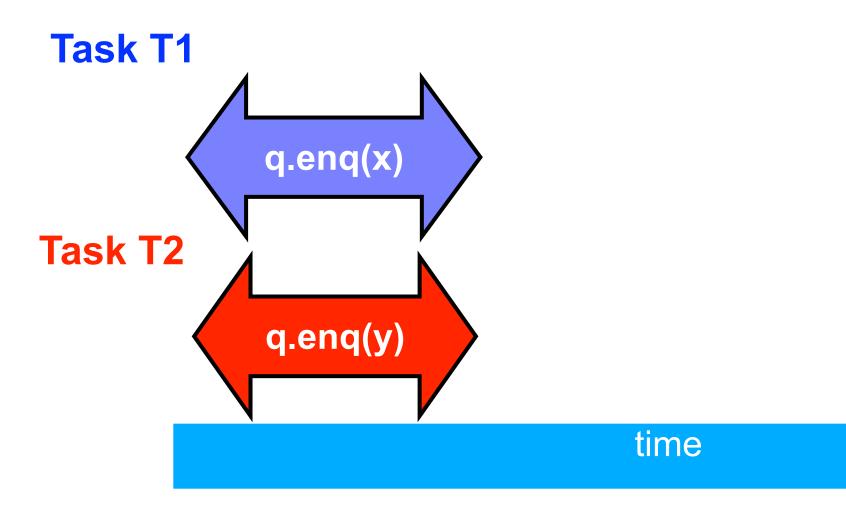
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Example 1

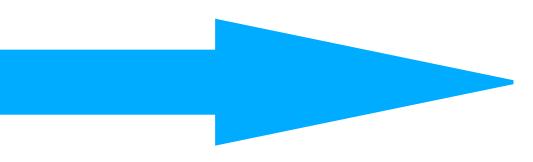




Example 1 cont.

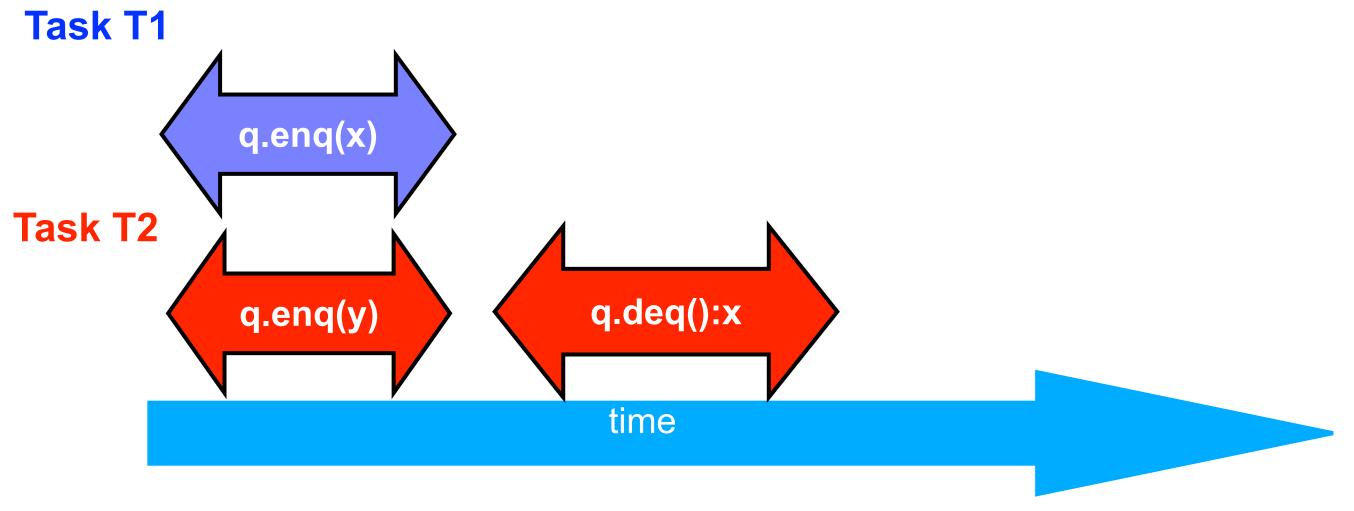


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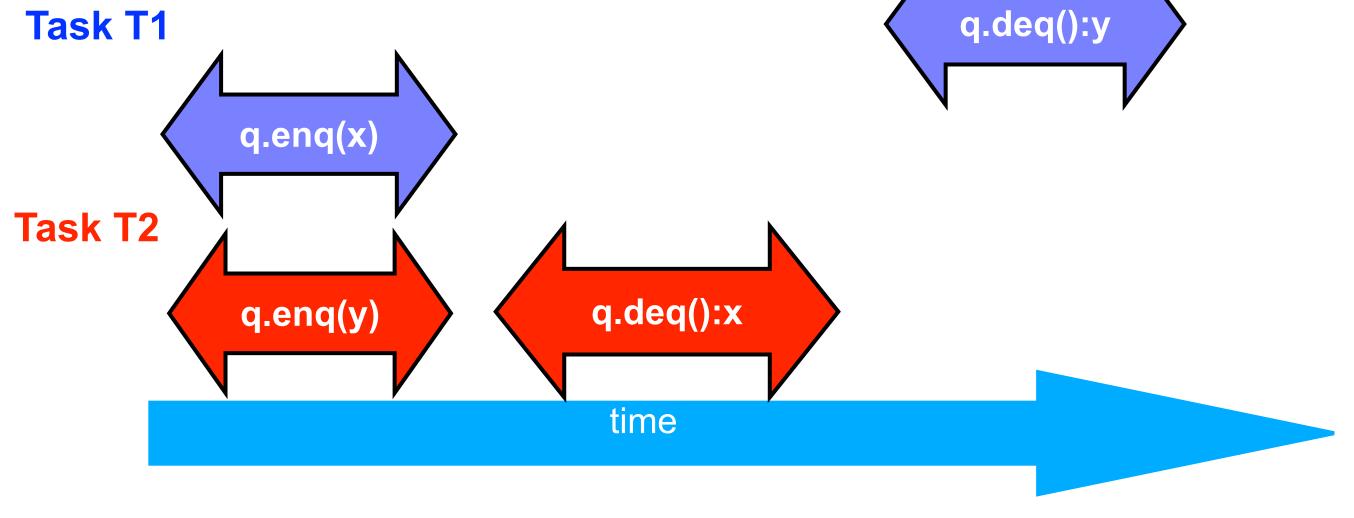


Example 1 cont.

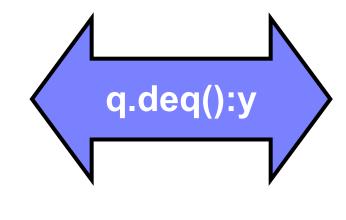


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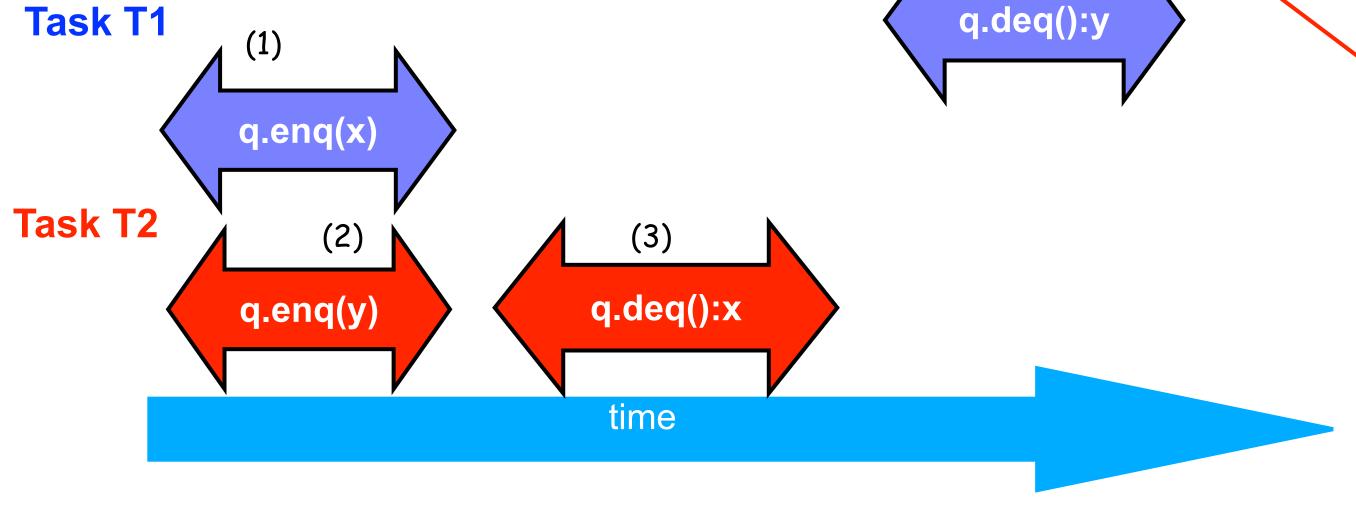


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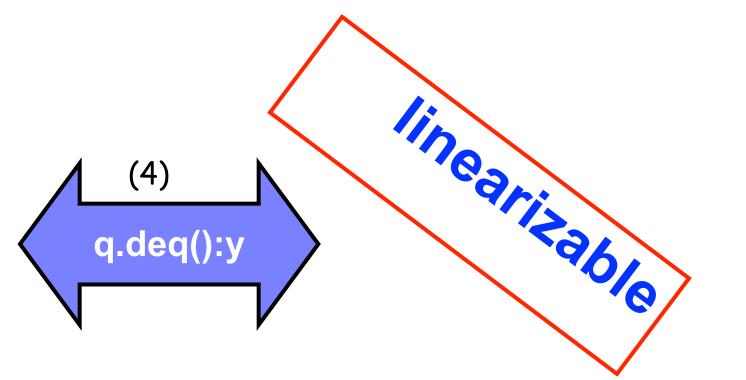




Example 1: is this execution linearizable?

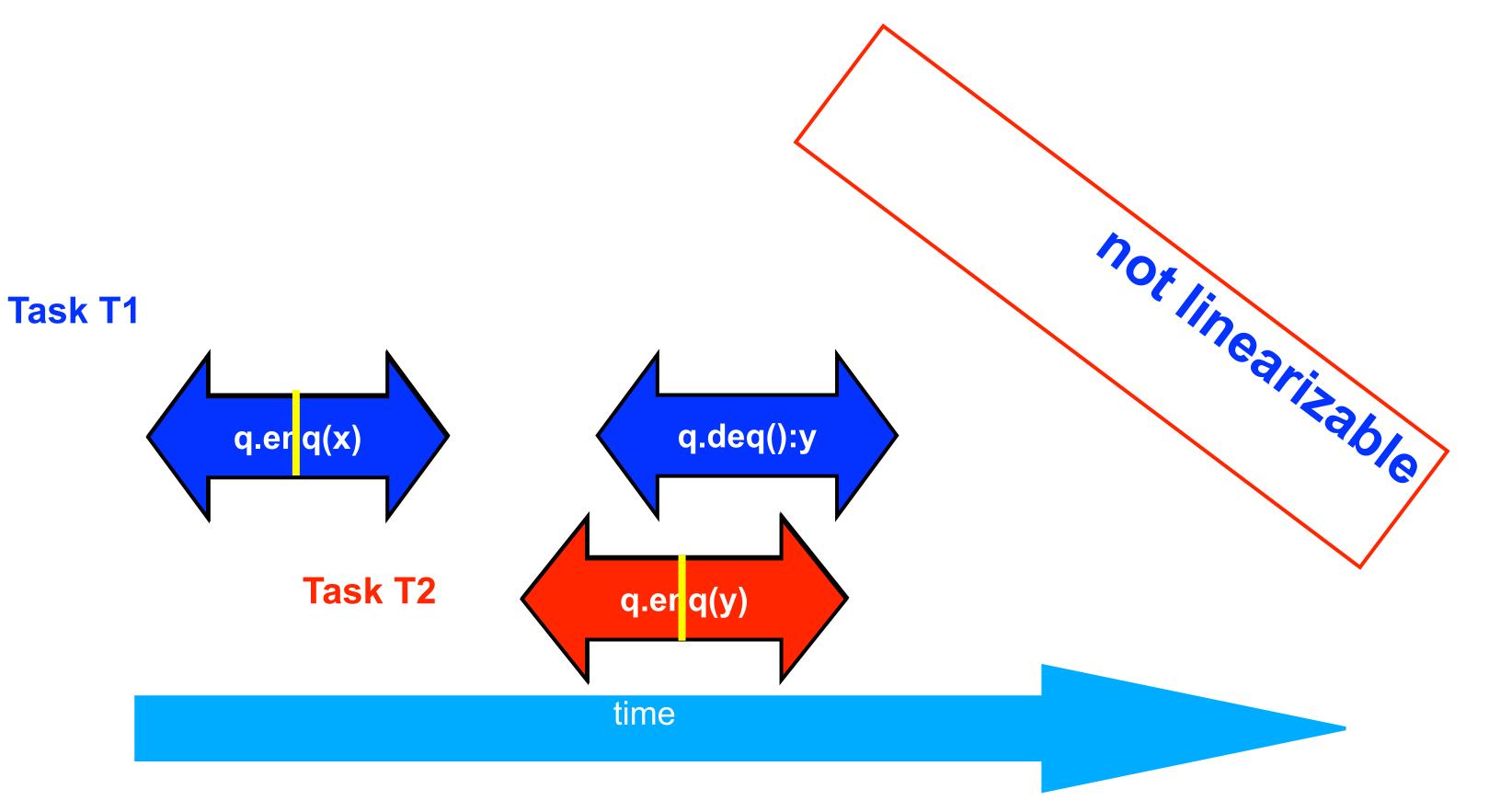


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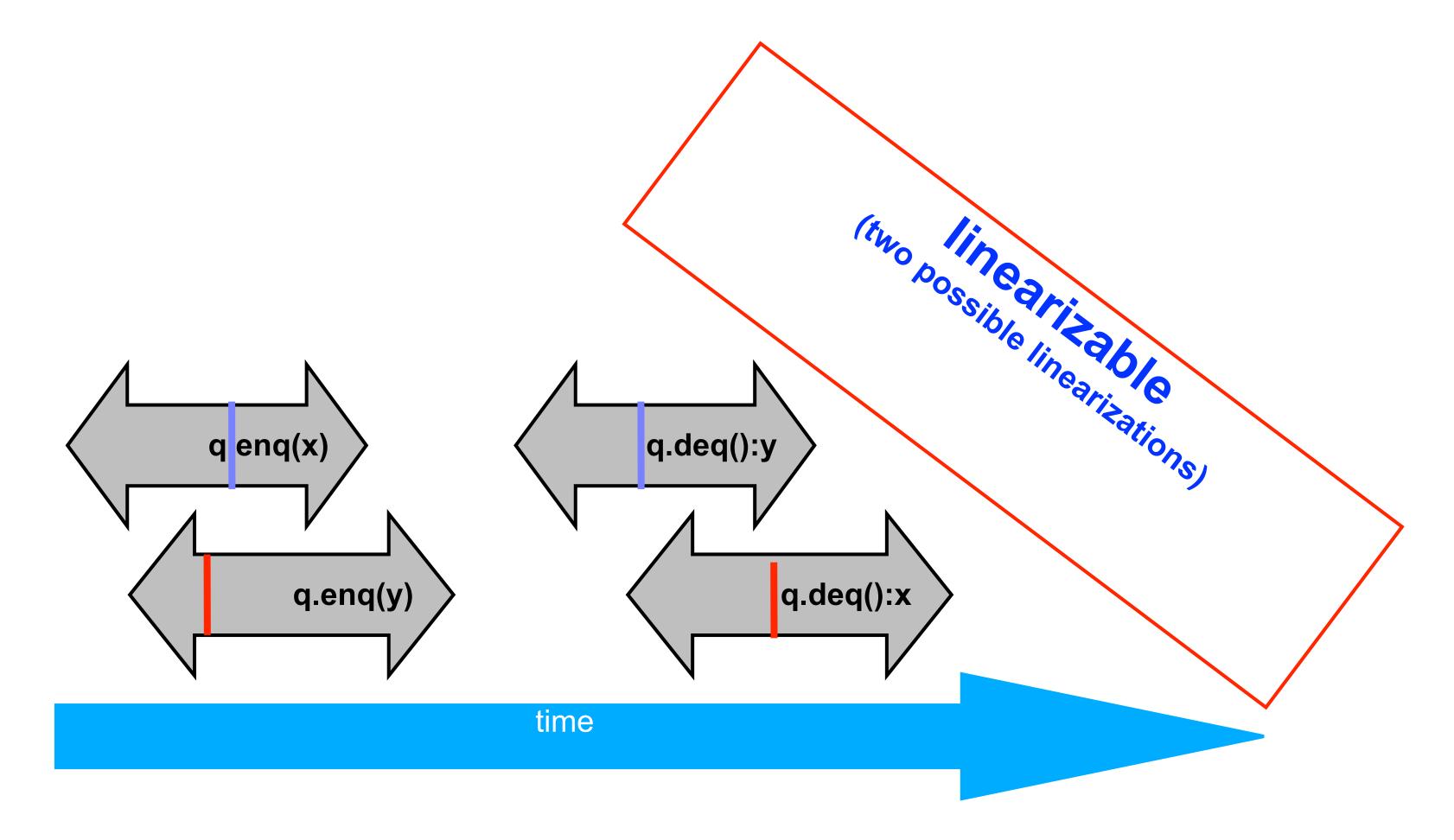
Example 2: is this execution linearizable?



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Is this execution linearizable? How many possible linearizations does it have?



Example 3

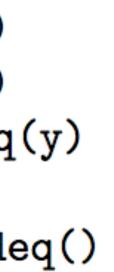


Example 4: execution of isolated implementation of FIFO queue q

Is this a linearizable execution?

Time	Task A	Task B
0	Invoke q.enq(x)	
1	Work on q.enq(x)	
2	Work on q.enq(x)	
3	Return from q.enq(x)	
4		Invoke q.enq(y)
5		Work on q.enq(y)
6		Work on q.enq(y)
7		Return from q.enq
8		Invoke q.deq()
9		Return x from q.de

Yes! Can be linearized as "q.enq(x) ; q.enq(y) ; q.deq():x"









Linearizability of Concurrent Objects (Summary)

Concurrent object

 A concurrent object is an object that can correctly handle methods invoked in parallel by different tasks or threads

—Examples: Concurrent Queue, AtomicInteger

Linearizability

- Assume that each method call takes effect "instantaneously" at some distinct point in time between its invocation and return.
- An <u>execution</u> is linearizable if we can choose instantaneous points that are consistent with a sequential execution in which methods are executed at those points
- An <u>object</u> is linearizable if all its possible executions are linearizable

