
COMP 515: Advanced Compilation for Vector and Parallel Processors

Vivek Sarkar
Department of Computer Science
Rice University
vsarkar@rice.edu

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COMP 515

Lecture 17

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Managing Cache

Allen and Kennedy, Chapter 9

Introduction

- **Register**
 - One word per register (typically, but there may be exceptions e.g., SIMD registers)
 - Temporal reuse
 - Direct store
 - Eviction (spills) managed by software

- **Cache**
 - Multiple words in a cache line, multiple lines in an associative set, multiple sets in a cache
 - Temporal and Spatial reuse
 - Load before store
 - Eviction managed by hardware (software can also help)

Spatial Reuse

- Permits high reuse when accessing closely located data

- `DO I = 1, M`

- `DO J = 1, N`

- `A(I, J) = A(I, J) + B(I, J)`

- `ENDDO`

- `ENDDO`

No reuse/locality for Fortran's column-major layout

Spatial Reuse (after loop interchange)

- DO J = 1, N
 DO I = 1, M
 A(I, J) = A(I, J) + B(I, J)
 ENDDO
ENDDO

Iterates over columns instead

Temporal Reuse

- Reuse limited by cache size, LRU replacement strategy
- `DO I = 1, M`
 - `DO J = 1, N`
 - `A(I) = A(I) + B(J)`
 - `ENDDO`
- `ENDDO`

Temporal Reuse

- Strip mining + Interchange (or Tiling) can improve temporal reuse when tile size S is chosen so that inner loops can fit in cache
- ```
DO J = 1, N, S
 DO I = 1, M
 DO jj = J, MIN(N, J+S-1)
 A(I) = A(I) + B(jj)
 ENDDO
 ENDDO
ENDDO
```

# Loop Interchange

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- Which loop should be innermost ?
- Strives to reduce distances between memory accesses to increase locality
- Attaches cost function to the loop and computes for best loop ordering



# Cost Assignment

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- Consider cost analysis for an innermost loop with  $N$  iterations, for arrays with element size =  $S$  bytes, and a cache with line size =  $L$  bytes
- Cost is 1 for references that do not depend on loop induction variables
- Cost is  $N$  for references based on induction variables over a non-contiguous space
- Cost is  $N*S/L$  for induction variables based references over contiguous space

# Loop Reordering

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- Once the cost is established, reorder the loop from cheapest innermost loop to high cost outermost loop

# Loop Blocking (Tiling)

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- DO J = 1, M  
    DO I = 1, N  
        D(I) = D(I) + B(I,J)  
    ENDDO  
ENDDO

$NM/b$  misses for each of arrays B and D

$\Rightarrow$  total of  $2NM/b$  misses

$b$  = block (line) size in words (elements)

Assume that N is large enough for elements of D to overflow cache

# Blocking loop I

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- After strip-mine-and-interchange

```
DO II = 1, N, S
```

```
 DO J = 1, M
```

```
 DO I = II, MIN(II+S-1, N)
```

```
 D(I) = D(I) + B(I,J)
```

```
 ENDDO
```

```
 ENDDO
```

```
ENDDO
```

$NM/b + N/b = (1 + 1/M) NM / b$  misses

Assume that  $S$  is  $\geq b$  and is also small enough to allow  $S$  elements of  $D$  to be held in cache for all iterations of the  $J$  loop

# Blocking Loop J

---

```
• DO J = 1, M, T
 DO I = 1, N
 DO jj = J, MIN(J+T-1, M)
 D(I) = D(I) + B(I, jj)
 ENDDO
 ENDDO
ENDDO
```

$NM/b$  misses for array B (if T is small enough)

$(N/b)*(M/T)$  misses for array D

$\Rightarrow$  Total of  $(1 + 1/T) NM/b$  misses

# Legality of Blocking

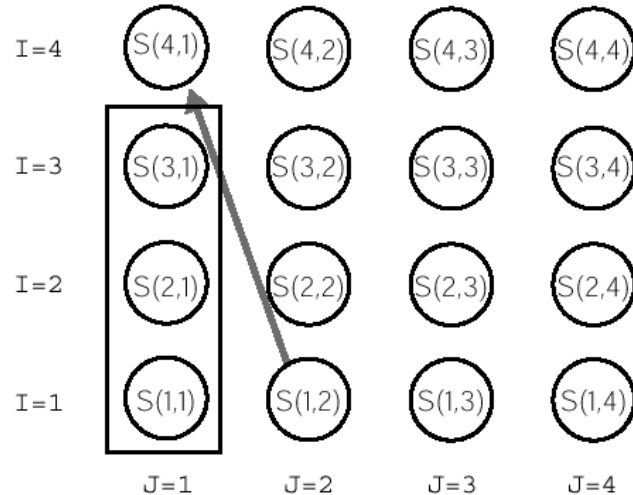
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- **Strip mining is always legal**
- **Loop interchange is not always legal**

```
procedure StripMineAndInterchange (L, m, k, o, S)
 // L = {L1, L2, ..., Lm} is the loop nest to be transformed
 // Lk is the loop to be strip mined
 // Lo is the outer loop which is to be just inside the by-strip loop
 // after interchange
 // S is the variable to use as strip size; it's value must be positive
 let the header of Lk be
 DO I = L, N, D;
 split the loop into two loops, a by-strip loop:
 DO I = L, N, S*D
 and a within-strip loop:
 DO i = I, MAX(I+S*D-D, N), D
 around the loop body;
 interchange the by-strip loop to the position just outside of Lo;
end StripMineAndInterchange
```

# Legality of Blocking

- Every direction vector for a dependence carried by any of the loops  $L_0 \dots L_{k+1}$  has either an “=” or a “<” in the  $k$ th position
- Conservative testing



# Profitability of Blocking

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- Profitable if there is reuse between iterations of a loop that is not the innermost loop
- Reuse occurs when:
  - There's a small-threshold dependence of any type, including input, carried by the loop (temporal reuse), or
  - The loop index appears, with small stride, in the contiguous dimension of a multidimensional array and in no other dimension (spatial reuse)



# Triangular Cache Blocking

---

- DO I = 2, N  
    DO J = 1, I-1  
        A(I, J) = A(I, I) + A(J, J)  
    ENDDO  
ENDDO

# Triangular Cache Blocking

---

- Applying strip mining
  - `DO I = 2, N, K`
    - `DO ii = I, I+K-1`
      - `DO J = 1, ii - 1`
        - $A(ii, J) = A(ii, I) + A(ii, J)$
- `ENDDO`
- `ENDDO`
- `ENDDO`

# Triangular Cache Blocking

---

- Applying triangular loop interchange

- `DO I = 2, N, K`

- `DO J = 1, I+K-1`

- `DO ii = MAX(J+1, I), I+K-1`

- `A(ii, J) = A(ii, I) + A(ii, J)`

- `ENDDO`

- `ENDDO`

- `ENDDO`

# Summary

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- Two different kind of reuse
  - Temporal reuse
  - Spatial reuse
- Strategies to increase the two reuse
  - Loop Interchange
  - Cache Blocking