COMP 322: Fundamentals of Parallel Programming

Lecture 6: Memoization

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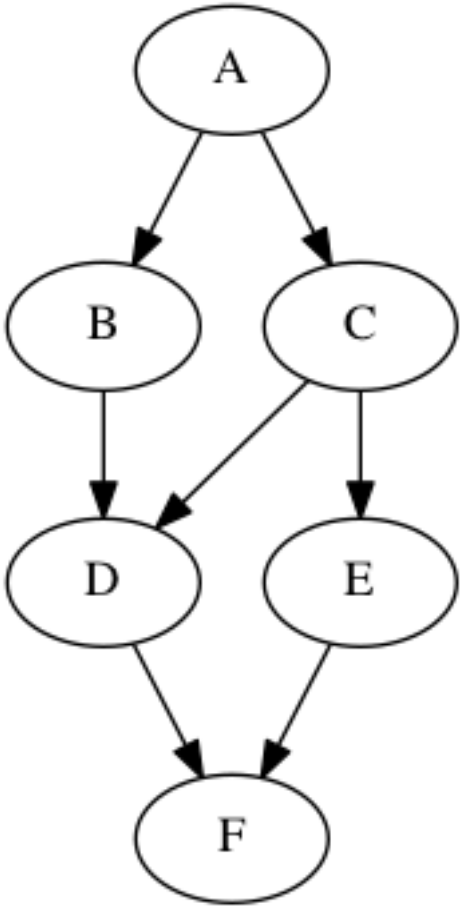
Worksheet #5: Computation Graphs for Async-Finish and Future Constructs

1) Can you write pseudocode with async-finish constructs that generates a Computation Graph with the same ordering constraints as the graph on the right? If so, provide a sketch of the program.

No. Finish cannot be used to ensure that D waits for both B and C, while E waits only for C.

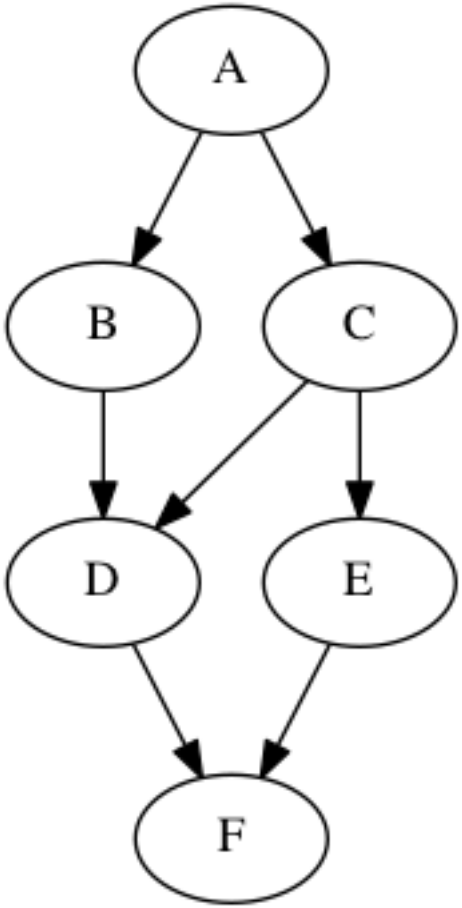
2) Can you write pseudocode with future async-get constructs that generates a Computation Graph with the same ordering constraints as the graph on the right? If so, provide a sketch of the program.

Yes, see program sketch with void futures. A dummy return value can also be used.



Worksheet #5 solution (contd)

```
1.  HjFuture<String> A = future(() -> {
2.      return "A"; });
3.  HjFuture<String> B = future(() -> {
4.      A.get(); return "B"; });
5.  HjFuture<String> C = future(() -> {
6.      A.get(); return "C"; });
7.  HjFuture<String> D = future(() -> {
8.      // Order of B.get() & C.get() doesn't matter
9.      B.get(); C.get(); return "D"; });
10. HjFuture<String> E = future(() -> {
11.     C.get(); return "E"; });
12. HjFuture<String> F = future(() -> {
13.     D.get(); E.get(); return "F"; });
14. F.get();
```



Background: Functional Programming

- Eliminate side-effects
  - emphasizes functions whose results that depend only on their inputs and not on any other program state
  - calling a function, f(x), twice with the same value for the argument x will produce the same result both times

Helpful Link: http://en.wikipedia.org/wiki/Functional_programming

Example: Binomial Coefficient

- The coefficient of the x^k term in the polynomial expansion of the binomial power $(1 + x)^n$
- Number of sets of k items that can be chosen from n items
- Indexed by *n* and *k*
  - written as C(n, k)
  - read as "n choose k"
- Factorial Formula: C(n, k) = $\left(\frac{n!}{k!(n-k)!} \right)$
- Recursive Formula

  C(n, k) = C(n – 1, k – 1) + C(n – 1, k)

  Base cases: C(n, n) = C(n, 0) = C(0, k) = 1

Helpful Link: http://en.wikipedia.org/wiki/Binomial_coefficient

Example: Binomial Coefficient (Recursive Sequential version)

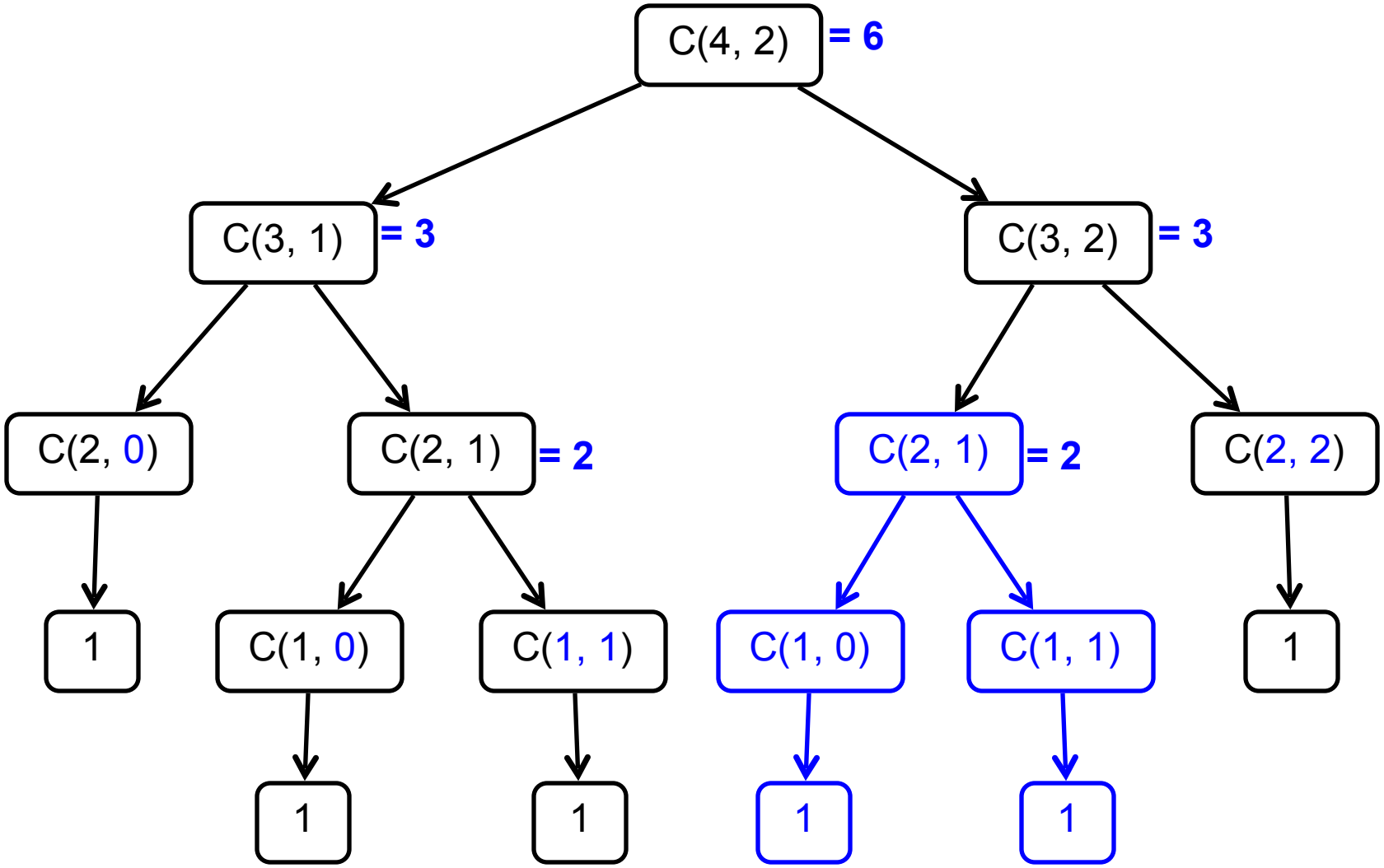
```
1.  int choose(int N, int K) {
2.      if (N == 0 || K == 0 || N == K) {
3.          return 1;
4.      }
5.      int left  = choose (N-1, K - 1);
6.      int right = choose (N-1, K);
7.      return left + right;
8.  }
```


Example: Binomial Coefficient (Parallel Recursive Pseudocode)

```
1.  Integer choose(int N, int K) {
2.      if (N == 0 || K == 0 || N == K) {
3.          return 1;
4.      }
5.      future<Integer> left  =
6.              future { return choose (N-1, K-1); }
7.      future<Integer> right =
8.              future { return choose (N-1, K); }
9.      return left.get() + right.get();
10. }
```

- Use of futures supports incremental parallelization with low developer effort

What inefficiencies do you see in the recursive Binomial Coefficient algorithm?



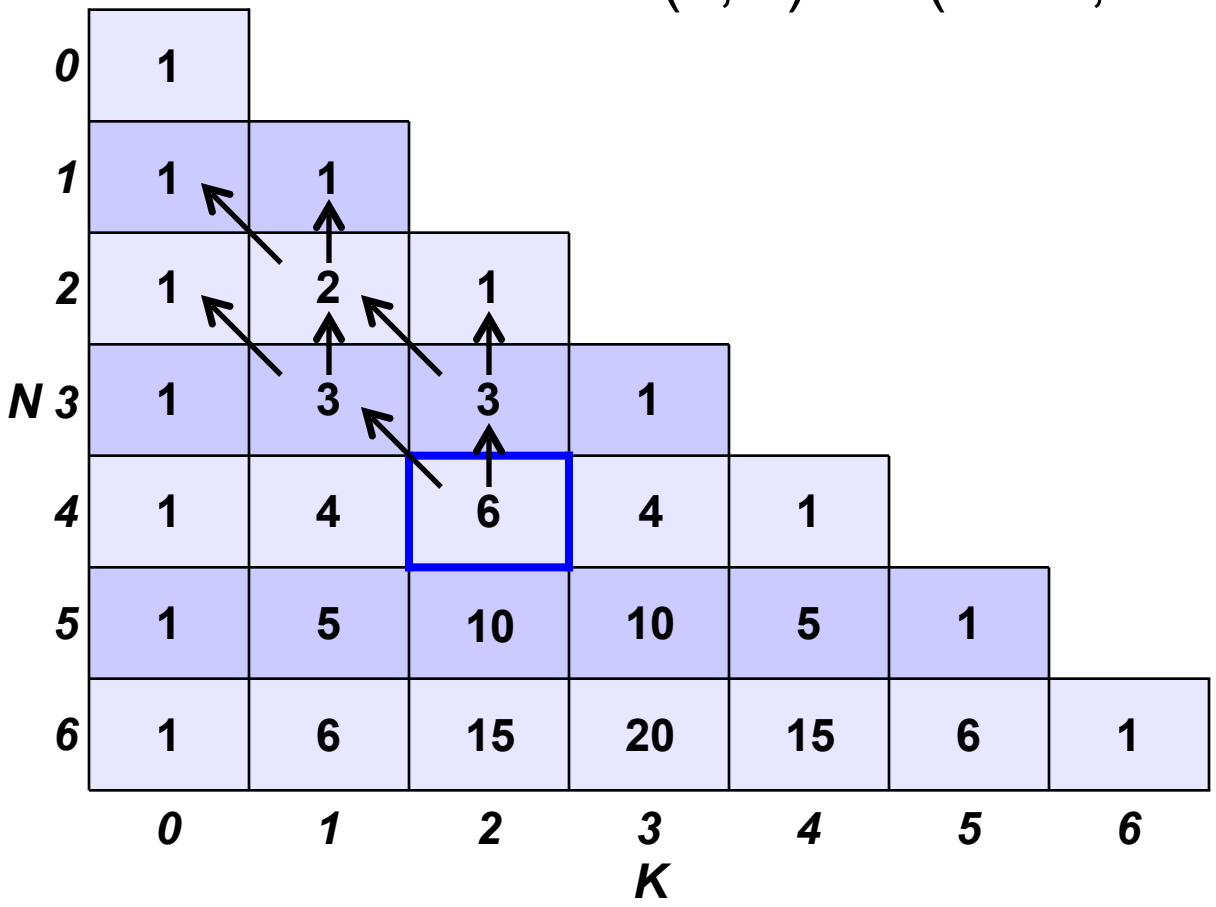
Memoization

- Memoization - saving and reusing previously computed values of a function rather than recomputing them
  - A optimization technique with space-time tradeoff
- A function can only be memoized if it is *referentially transparent*, i.e. functional
- Related to caching
  - memoized function "remembers" the results corresponding to some set of specific inputs
  - memoized function populates its cache of results transparently on the fly, as needed, rather than in advance

Helpful Link: http://en.wikipedia.org/wiki/Memoization

Pascal's Triangle is an example of Memoization

$$C(n, k) = C(n - 1, k - 1) + C(n - 1, k)$$



Example: Binomial Coefficient (sequential memoized version)

```
1.  final Map<Pair<Int, Int>, Int> cache = new ...;

2.  int choose(int N, int K) {
3.      Pair<Int, Int> key = Pair.factory(N, K);
4.      if (cache.contains(key)) {
5.          return cache.get(key);
6.      }
7.      if (N == 0 || K == 0 || N == K) {
8.          return 1;
9.      }
10.     int left  = choose (N - 1, K - 1);
11.     int right = choose (N - 1, K);
12.     int result = left + right;
13.     cache.put(key, result);
14.     return result;
15. }
```


Example: Binomial Coefficient (parallel memoized version w/ futures)

```
1.  final Map<Pair<Int, Int>, future<Integer>> cache = new ...;
2.  Integer choose(final int N, final int K) {
3.      final Pair<Int, Int> key = Pair.factory(N, K);
4.      if (cache.contains(key)) {
5.          return cache.get(key).get();
6.      }
7.      future<Integer> f = future {
8.        if (N == 0 || K == 0 || N == K) return 1;
9.        future<Integer> left = future { return choose (N-1, K-1); }
10.       future<Integer> right = future { return choose (N-1, K); }
12.       return left.get() + right.get();
13.     }
14.     cache.put(key, f);
15.     return f.get();
16. }
```

- Assumes availability of a "thread-safe" cache library, e.g., ConcurrentHashMap

Announcements & Reminders

- **IMPORTANT:**
  - **—Watch video & read handout for topic 2.3 for next lecture on Wednesday, Jan 23rd**
- **HW1 was posted on the course web site (http://comp322.rice.edu) on Jan 9th, and is due on Jan 23rd**
- **Quiz for Unit 1 (topics 1.1 - 1.5) is due by Jan 25th on Canvas**
- **See course web site for all work assignments and due dates**
- **Use Piazza (public or private posts, as appropriate) for all communications re. COMP 322**
- **See Office Hours link on course web site for latest office hours schedule.**