Chunking Parallel Loops in the Presence of Synchronization

Jun Shirako
Dept. of CS, Rice University
6100 Main St, Houston TX, USA
shirako@rice.edu

Jisheng Zhao
Dept. of CS, Rice University
6100 Main St, Houston TX, USA
jisheng.zhao@rice.edu

Vivek Sarkar
Dept. of CS, Rice University
6100 Main St, Houston TX, USA
vsarkar@rice.edu

V. Krishna Nandivada IBM India Research Laboratory EGL, Bangalore, 560071, India nvkrishna@in.ibm.com

ABSTRACT

Modern languages for shared-memory parallelism are moving from a bulk-synchronous Single Program Multiple Data (SPMD) execution model to lightweight Task Parallel execution models for improved productivity. This shift is intended to encourage programmers to express the *ideal* parallelism in an application at a fine granularity that is natural for the underlying domain, while delegating to the compiler and runtime system the job of extracting coarser-grained *useful* parallelism for a given target system. A simple and important example of this separation of concerns between ideal and useful parallelism can be found in *chunking* of parallel loops, where the programmer expresses ideal parallelism by declaring all iterations of a loop to be parallel and the implementation exploits useful parallelism by executing iterations of the loop in sequential *chunks*.

Though chunking of parallel loops has been used as a standard transformation for several years, it poses some interesting challenges when the parallel loop may directly or indirectly (via procedure calls) perform synchronization operations such as barrier, signal or wait statements. In such cases, a straightforward transformation that attempts to execute a chunk of loops in sequence in a single thread may violate the semantics of the original parallel program. In this paper, we address the problem of chunking parallel loops that may contain synchronization operations. We present a transformation framework that uses a combination of transformations from past work (e.g., loop strip-mining, interchange, distribution, unswitching) to obtain an equivalent set of parallel loops that chunk together statements from multiple iterations while preserving the semantics of the original parallel program. These transformations result in reduced synchronization and scheduling overheads, thereby improving performance and scalability. Our experimental results for 11 benchmark programs on an Ul-

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traSPARC II multicore processor showed a geometric mean speedup of $0.52\times$ for the unchunked case and $9.59\times$ for automatic chunking using the techniques described in this paper. This wide gap underscores the importance of using these techniques in future compiler and runtime systems for programming models with lightweight parallelism.

Categories and Subject Descriptors

D.1.3 [**Programming Techniques**]: Concurrent Programming; D.3.4 [**Programming Languages**]: Processors

General Terms

Algorithms, Languages, Performance

1. INTRODUCTION

Historically, the most successful runtimes for shared memory multiprocessors have been based on bulk-synchronous Single Program Multiple Data (SPMD) execution models [6]. OpenMP [17] represents one such embodiment in which the programmer's view of the runtime is that of a fixed number of threads executing tasks in "work-sharing" parallel constructs. However, modern languages such as Cilk [4], Chapel [13], Fortress [1], and X10 [5] have moved from SPMD to lightweight dynamic Task Parallel execution models for improved programmer productivity. This shift is intended to encourage programmers to express the ideal parallelism in an application at a fine granularity that is natural for the underlying domain, while delegating to the compiler and runtime system the job of extracting coarser-grained useful parallelism for a given target system. A simple and important example of this separation of concerns between ideal and useful parallelism can be found in chunking of parallel loops, where the programmer expresses ideal parallelism by declaring all iterations of a loop to be parallel and the implementation exploits useful parallelism by executing iterations of the loop in sequential *chunks* [15, 18]. In models like OpenMP, the programmer can guide the implementation by providing chunk policy and chunk size values that can be set dynamically for different platforms.

Though chunking of parallel loops has been employed as a standard transformation for several years, it poses some interesting challenges when the parallel loop may directly or indirectly (via procedure calls) perform *synchronization*

```
delta = epsilon+1; iters = 0;
#pragma omp parallel for
for (int j = 1 ; j <= n ; j++ ) {
    while ( delta > epsilon ) {
        newA[j] = (oldA[j-1]+oldA[j+1])/2.0 ;
        diff[j] = abs(newA[j]-oldA[j]);
        #pragma omp barrier
        if (j == 1) {
            delta = sum(diff); iters++;
            temp = newA; newA = oldA; oldA = temp;
        }
        #pragma omp barrier
    }
}
```

Figure 1: One-Dimensional Iterative Averaging Example in Non-conformable OpenMP C

```
delta = epsilon+1; iters = 0;
phaser ph = new phaser(single);
foreach ( point[j] : [1:n] ) phased(single(ph)) {
    while ( delta > epsilon ) {
        newA[j] = (oldA[j-1]+oldA[j+1])/2.0 ;
        diff[j] = Math.abs(newA[j]-oldA[j]);
        next { // barrier with single statement
        delta = diff.sum(); iters++;
        temp = newA; newA = oldA; oldA = temp;
    } } }
```

Figure 2: One-Dimensional Iterative Averaging Example in X10 with Phasers

operations such as barrier, signal or wait statements. In such cases, a straightforward transformation that attempts to execute a chunk of loop iterations in sequence in a single thread may violate the semantics of the original program.

For example, consider the OpenMP code fragment in Figure 1. It embodies the pedagogical One-Dimensional Iterative Averaging program from [7]. The goal of this program is to perform iterative averaging on an one-dimensional array A. As shown in Figure 1, the program does not conform with the OpenMP specification because OpenMP prohibits a barrier region from being nested inside a loop region. This restriction harks back to the basic bulk-synchronous nature of SPMD computations. Attempting to run the OpenMP code in Figure 1 yields unpredictable results on different platforms ranging from deadlock to runtime error messages (but no compile-time error messages).

Even though illegal in OpenMP, the intent behind the code in Figure 1 is clear enough. The programmer wishes to create a parallel j loop with n iterations, in which each parallel iteration consists of a sequential while loop. Barrier operations are inserted to ensure that different j iterations synchronize with each other before advancing to the next iteration of the while loop, and that new values of delta and iters are computed by the j=1 iteration between the two barriers. Modern languages such as Chapel [13], Fortress [1], and X10 [5] support this form of synchronization with finegrained dynamic parallelism. We show the X10 version in Figure 2 using the phasers extension described in [20]. The

```
delta = epsilon+1; iters = 0;
phaser ph = new phaser(single);
foreach ( point[jj] : [1:n:S] ) phased(single(ph)) {
  for (int j = jj ; j <= min(jj+S-1,n) ; j++) {
    while ( delta > epsilon ) {
      newA[j] = (oldA[j-1]+oldA[j+1])/2.0 ;
      diff[j] = Math.abs(newA[j]-oldA[j]);
      next { // barrier with single statement
       delta = diff.sum(); iters++;
      temp = newA; newA = oldA; oldA = temp;
    } } } }
```

Figure 3: Naive (Incorrect) Chunking of X10 version from Figure 2

parallel j loop is now expressed as a foreach statement in X10. All iterations of the foreach are registered on the same phaser variable, ph. The next statement serves as a barrier with a *single* statement [25] that is guaranteed to be executed by only one thread.

The code in Figure 2 correctly captures the programmer's intent. However, if n is larger than the number of available hardware threads, this code can incur significant overhead since the barrier synchronization performed by the phaser involves all n iterations. As indicated earlier, loop chunking is a standard approach to improve the efficiency of a parallel loop. Figure 3 shows the result of performing a chunking transformation mechanically on the foreach loop, with the goal of decomposing the foreach loop into chunks of S iterations². However, though this chunking transformation is legal for parallel loops that do not contain synchronization operations, it is not legal for the example in Figure 2 since it contains a next (barrier) operation. In particular, the transformed version (Figure 3) will attempt to complete all iterations of the while loop for iteration j before starting iteration j+1 from the same chunk, which is different from the semantics of the original code in Figure 2. A similar problem would arise if the original foreach loop contained signal and wait operations instead of barrier operations.

In this paper, we address the problem of chunking parallel loops that may contain synchronization operations. We present a transformation framework that uses a combination of transformations from past work (e.g., loop strip-mining, interchange, distribution, unswitching) to obtain an equivalent set of parallel loops that chunk statements from multiple iterations while preserving the semantics of the original program. These transformations result in reduced synchronization and scheduling overheads, thereby improving performance and scalability. Our experimental results for 11 benchmark programs on an UltraSPARC II multicore processor showed a geometric mean speedup of $0.52\times$ for the unchunked case and $9.59\times$ for automatic chunking using the techniques described in this paper. This wide gap underscores the importance of using these techniques in compiler and runtime systems for programming models with lightweight parallelism. A hand-coded study of different chunking policies for two benchmarks revealed the potential for even greater performance improvements in the future.

ble to any language that permits synchronization operations to occur in a parallel loop.

²The 1:n:S notation in the new jj foreach loop is akin to the *low*: *high*: *stride* triple notation in Fortran 90 [16].

¹While X10 is the language used to describe the problem and our solution, the approach described in this paper is applica-

The rest of the paper is organized as follows. Section 2 includes background on X10 and on classical loop transformations. Section 3 describes the loop chunking transformation framework. Section 4 discusses how the framework in Section 3 can be extended to support exceptions. Section 5 contains our experimental results. Section 6 discusses related work, and Section 7 contains our conclusions.

2. BACKGROUND

2.1 X10 and Phasers

This section provides a brief summary of the async, finish, and foreach constructs introduced in v0.41 of the X10 programming language [5], as well as the phasers extension from [20]. Additional X10 constructs such as places and futures that are not central to the paper have been omitted.

2.1.1 $async \langle stmt \rangle$

Async is the X10 construct for creating or forking a new asynchronous activity. The statement, $async \langle stmt \rangle$, causes the parent activity to create a new child activity to execute $\langle stmt \rangle$. Execution of the async statement returns immediately i.e., the parent activity can proceed immediately to its following statement.

2.1.2 $finish \langle stmt \rangle$

The X10 statement, $finish \langle stmt \rangle$, causes the parent activity to execute $\langle stmt \rangle$ and then wait till all sub-activities created within $\langle stmt \rangle$ have terminated (including transitively spawned activities). Operationally, each instruction executed in an X10 activity has a unique $Immediately\ Enclosing\ Finish$ (IEF) dynamic statement instance.

Besides termination detection, the finish statement plays an important role with regard to exception semantics. An X10 activity may terminate normally or abruptly. A statement terminates abruptly when it throws an exception that is not handled within its scope; otherwise it terminates normally. X10 requires that if statement S or an activity spawned by S terminates abruptly, and all activities spawned by S terminate, then finish S terminates abruptly and throws a single exception formed from the collection of all exceptions thrown by S or its descendant activities.

2.1.3 Foreach

The statement foreach (point p: R) S supports parallel iteration over all the points in region R by launching each iteration as a separate async. A point is an element of an n-dimensional Cartesian space ($n \geq 1$) with integer-valued coordinates. A region is a set of points, and can be used to specify an array allocation or iteration constructs as in the case of foreach. For instance, the region [0:200,1:100] specifies a collection of two-dimensional points (i,j) with i ranging from 0 to 200 and j ranging from 1 to 100.

A foreach statement does not have an implicit finish (join) operation, but its termination can be ensured by enclosing it within a finish statement at an appropriate outer level. Further, any exceptions thrown by the spawned iterations are propagated to its IEF instance.

2.1.4 Phasers

In this section, we summarize the *phaser* construct introduced in [20] as an extension to X10 *clocks* [5]. Phasers inte-

grate collective and point-to-point synchronization by giving each activity (task) the option of registering with a phaser in signal-only/wait-only mode for producer/consumer synchronization or signal-wait mode for barrier synchronization. In addition, a next statement for phasers can optionally include a *single* statement (as in Figure 2) which is guaranteed to be executed exactly once during a phase transition [25]. These properties, along with the generality of dynamic parallelism and the phase-ordering and deadlock-freedom safety properties, distinguish phasers from synchronization constructs in past work including barriers [11, 17], counting semaphores [19], and X10's clocks [5]. Though phasers as described in this paper may seem X10-specific, they are a general unification of point-to-point and collective synchronizations that can be added to any programming model with dynamic parallelism such as OpenMP [17], Intel's Thread Building Blocks, Microsoft's Task Parallel Library, and Java Concurrency Utilities [10].

A phaser is a synchronization object that supports the following five operations by an activity A_i :

- new: When A_i performs a new phaser (MODE) operation, it results in the creation of a new phaser ph such that A_i is registered with ph according to MODE.
- **drop:** A_i drops its registration on all phasers when it terminates. In addition, when A_i executes an end-finish instruction for **finish** statement F, it completely de-registers from each phaser ph for which F is the IEF for ph's creation. This constraint is necessary for the deadlock freedom property for phasers [20].
- **next:** The **next** operation has the effect of advancing each phaser on which A_i is registered to its next phase, thereby synchronizing all activities registered on the same phaser. The semantics of **next** depends on the registration mode that A_i has on each phaser, thereby making it possible for the **next** statement to be used for both barrier and point-to-point synchronizations [20].
- signal: A signal operation performed by A_i is shorthand for a ph.signal() operation performed on each phaser ph with which A_i is registered with a signal capability.
- wait: Like next, the wait operation has the effect of advancing each phaser that A_i is registered on to its next phase. However unlike next, the wait operation does not include signal operations on any phasers.

2.2 Classical Loop Transformations

This section briefly summarizes some classical loop restructuring techniques that have historically been used to improve parallelism and data locality, and expose other opportunities for compiler optimization [23, 14]:

- Strip Mining is a loop transformation that fragments a single loop into two nested loops with smaller segments. This restructuring is an important preliminary step for vectorization, tiling, SIMDization, and other transformations for improving locality and parallelism.
- Loop Interchange results in a permutation of the order of loops in a loop nest, and can be used to improve data locality, coarse-grained parallelism and vectorization opportunities.
- Loop Distribution divides the body of a loop and generates several loops for different parts of the loop body. This transformation can be used to convert loop-carried dependences to loop-independent dependences, thereby exposing more parallelism.

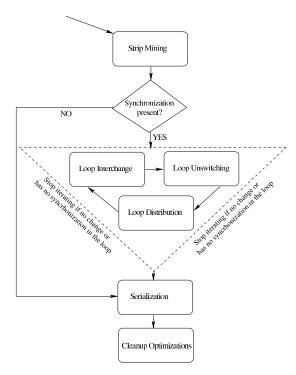


Figure 4: Block diagram for Transformation Framework

• Loop Unswitching is akin to interchanging a loop and a conditional construct. If the condition value is loop-invariant it can be moved outside so that it is not evaluated in every iteration.

The legality constraints for these transformations are well understood for the case when the input program is sequential. In Sections 3 and 4, we show how these transformations can be extended to enable chunking of parallel loops in the presence of synchronizations and exceptions.

3. TRANSFORMATION FRAMEWORK

In this section we present our transformation framework to enable chunking of foreach loops containing synchronization operations. To simplify the presentation, this section will focus on the restricted case when the loop body is known to be exception-free. Section 4 discusses how the framework in this section can be extended to support exceptions. The synchronization operation that we will focus on in this description is the next statement for clocks and phasers; as mentioned in Section 2.1, the phaser next statement can be used to support both barrier and point-to-point synchronizations.

Figure 4 shows a block diagram for our transformation framework. The general strategy to chunk parallel loops containing synchronization operations is as follows. The foreach loop is first strip-mined into two nested parallel loops. If the loop body contains no next statements, then the inner loop can be serialized and a chunked version can be obtained after performing some clean-up transformations (the "No" case in the flow chart). If the loop body contains next statements, then a combination of three transformations — loop distribution, loop interchange, and loop unswitching — is applied repeatedly until a) no next state-

Figure 5: Example foreach loop containing next statements

ments occur inside any instance of an inner foreach loop or b) no further change is possible. In case a), we can proceed to the serialization and clean-up transformations as before to obtain a chunked parallel loop. In case b), the compiler is unable to chunk the parallel loop and the foreach statement is left unchanged. The motivation for selecting loop distribution, loop interchange, and loop unswitching as the three transformations to iterate on is to attempt to isolate the next statements by moving the inner parallel loop as far inwards as possible. These three transformations used in this framework are monotonic — though they may be applied in any order, the resulting transformed code is guaranteed to be deterministic. Of these three transformations, the Loop distribution is the basic transformation needed for chunking by isolating next operations. Interchange and unswitching increase the opportunities for isolation. Next contraction and choice of chunking policy are used to improve the efficiency of the chunked version. In this work, we assume that all programmer-specified conditions guarding a next statement are *invariant* in the initial foreach loop i.e., the conditions are single-valued [25]. However, as we will see in Section 4, our transformation framework can handle cases when a next statement is guarded by implicit exception conditions.

Figure 5 contains an example foreach loop with next statements. In this example, all iterations of the foreach loop are registered in *signal-wait* mode on phaser ph, which means that the next statements serve as barrier operations. However, the transformation framework is also applicable to other phaser registration modes for which a next statement may result in point-to-point synchronizations instead of a barrier operation. It is obvious that a standard chunking of the foreach loop in Figure 5 will not be legal. The following sections describe the transformations performed by a framework that can lead to a legal chunking.

3.1 Strip Mining

The classical strip-mining transformation results in chunks of contiguous iterations. However, for generality, we will define strip-mining of a region (iteration space) R to be an ordered pair (Ig, Ie), where $\operatorname{Ig}(R)$ is an iterator over multiple chunks and for each chunk g, $\operatorname{Ie}(R,g)$ returns an iterator over the different indices in the chunk. In addition to the ability to specify chunks of non-contiguous iterations, this formulation allows us to specify chunking of multi-dimensional loops since regions can be multidimensional in X10. Figure 6 shows the iteration spaces for Block and Cyclic chunking policies for region R = [0:N-1] with P chunks.

Chunking Policy	Iteration Sets
Block	$\{0, 1, \dots N/P - 1\}, \{N/P, N/P + 1, \dots 2 \times N/P - 1\}, \dots, \{(P-1) \times N/P, \dots N - 1\}$
Cyclic	$\{0, P, \dots, \}, \{1, P+1, \dots, \}, \dots, \{P-1, 2 \times P-1, \dots, \}$

Figure 6: Iteration sets for Block and Cyclic chunking policies for region R = [0: N-1] and P chunks.

Figure 7: foreach Strip Mining Transformation Rule

Our rule for strip-mining foreach loops is shown in Figure 7. The i-foreach is a special "inner foreach" construct that is defined only for our transformation framework. It is not available to the programmer and it will not be present in the final output code. This new construct carries forward the dependence information and the exception semantics till we do the actual transformation. If chunking is successful, then all instances of i-foreach are replaced by sequential for loops; otherwise the original foreach loop remains unchanged. This all-or-nothing approach is proposed for simplicity; extensions to support partial chunking is a topic for future work. Also, the real benefit of chunking in practice will only be realized when it is performed across all statements in the original foreach, since even a single unchunked statement will result in the creation of a large number of fine-grained activities.

i-foreach represents a foreach loop with an *implicit finish* operation. This is in contrast to a normal foreach which is asynchronous by default and needs explicit finish operations. i-foreach also has an empty phased clause, which by definition registers on all the parent's phasers with the same modes as the parent activity [20] i.e., the outer foreach. Also, though transmission of clocks and phasers is not permitted through explicit finish operations in X10, it is permitted through the implicit finish in an i-foreach because we know that all i-foreach's will eventually be replaced by sequential loops if a chunking transformation is performed.

As shown in Figure 7, the strip-mining transformation is always legal since the inner i-foreach loop is still parallel. The fact that the inner i-foreach has an implicit finish does not limit the parallelism in the original loop. Figure 8 shows the result of the strip-mining transformation when applied to the code example in Figure 5 (the changes are shown in **bold** face).

3.2 Loop Interchange, Loop Unswitching, Loop Distribution, Next Contraction

Our serialization mechanism (described in Section 3.3) requires that no next operations appear in any i-foreach construct. In this section, we describe an iterative approach to either move all next operations out of the i-foreach loops targeted for serialization, or declare the original foreach loop to be non-chunkable. This approach is based on repeated applications of the transformations shown in Figure 9. We now briefly describe each rule in Figure 9 and summarize their assumptions. If any of the assumptions is not satisfied, then the rule cannot be applied and the com-

```
finish {
  ph = new phaser(); // SIG_WAIT mode by default
  foreach (point g: Ig(R)) phased(ph) {
    i-foreach (point i : Ie(R, g)) phased {
      for (int j = 0; j < m; j++) {
         S1;
         next;
      if (array[j] != 0) {
         for (int k = 0; k < 1; k++) {
            S2;
            next; } } }
}</pre>
```

Figure 8: Strip-mining of foreach loop in Figure 5.

piler will have to conclude that the original foreach loop cannot be chunked.

Rule 1 (Loop Interchange) builds on a well known observation from classical vectorization namely, "a loop that carries no dependences cannot carry any dependences that prevent interchange with other loops nested inside it" [14]. Though this observation was developed for sequential loops that are parallelizable, it is just as applicable to parallel i-foreach loops. Thus, the interchange in Rule 1 can be performed without the need for checking any data dependences. For simplicity, we assume that the inner sequential loop's iteration space, R2, is independent of the outer i-foreach loop's index variable. Extension of this rule to support interchange of trapezoidal loops should be straightforward as in past work on loop interchange in sequential programs [14]. We also assume that the loop body S does not contain any break or continue statements; support for those statements is more complicated, but can be built on the exception support in Section 4.

Rule 2 (*Loop Unswitching*) builds on the classical unswitching transformation for sequential code [14]. The main assumption here is that the condition e is independent of the i-foreach loop's index variable.

Rule 3 (Loop Distribution) builds on another well known observation that a parallel loop can always be fully distributed [14] since a loop-carried dependence is needed to create a distribution-preventing cycle. Hence the i-foreach loops can be fully distributed. The implicit finish operations in i-foreach ensure the correctness of the resulting transformation. As in classical loop distribution, it may be necessary in some cases to perform scalar expansion [14] on any iteration-private scalar variables that may be accessed in both \$1 and \$2.

```
1. Loop Interchange:
 i-foreach (point p : R1) phased
                                                           for (point q: R2)
    for (point q : R2)
                                                             i-foreach (point p : R1) phased
    // R2 is assumed to be independent of p
     S // S contains no break/continue statements
2. Loop Unswitching:
 i-foreach (point p : R1) phased
                                                           if (e)
    if (e)
                                                             i-foreach (point p : R1) phased
    // e is assumed to be independent of p
     S
3. Loop Distribution:
                                                           i-foreach (point p : R1) phased
 i-foreach (point p : R1) phased
    { S1; S2; }
                                                           i-foreach (point p : R1) phased
4. Next Contraction:
 i-foreach (point p : R1) phased
    // Region R1 is assumed to be non-empty.
                                                           next
```

Figure 9: Rules for Loop Interchange, Loop Unswitching, Loop Distribution, and Next Contraction

```
// After Loop Interchange
                                                      // After Loop Distribution
finish {
                                                      finish {
 ph = new phaser(); // SIG_WAIT mode by default
                                                        ph = new phaser(); // SIG_WAIT mode by default
 foreach (point g: Ig(R)) phased(ph) {
                                                        foreach (point g: Ig(R)) phased(ph) {
    for (int j = 0; j < m; j++) {
                                                          for (int j = 0; j < m; j++) {
      i-foreach (point i : Ie(R, g)) phased {
                                                             i-foreach (point i : Ie(R, g)) phased {
       S1;
                                                              S1; }
       next;
                                                             i-foreach (point i : Ie(R, g)) phased {
        if (array[j] != 0) {
                                                              next; }
                                                             i-foreach (point i : Ie(R, g)) phased {
         for (int k = 0; k < 1; k++) {
                                                              if (array[j] != 0) {
           for (int k = 0; k < 1; k++) {
                                                                  S2;
                                                                  next; } } } } }
                 (a)
                                                                       (b)
// After Next Contraction and Loop Unswitching
                                                      // After Loop Interchange, Loop Distribution,
                                                      // and Next Contraction
finish {
 ph = new phaser(); // SIG_WAIT mode by default
                                                      finish {
                                                        ph = new phaser(); // SIG_WAIT mode by default
 foreach (point g: Ig(R)) phased(ph) {
   for (int j = 0; j < m; j++) {
                                                        foreach (point g: Ig(R)) phased(ph) {
      i-foreach (point i : Ie(R, g)) phased {
                                                          for (int j = 0; j < m; j++) {
                                                            i-foreach (point i : Ie(R, g)) phased {
       S1; }
      next; // Contracted
                                                              S1; }
      if (array[j] != 0) {
                                                            next;
        i-foreach (point i : Ie(R, g)) phased {
                                                            if (array[j] != 0) {
         for (int k = 0; k < 1; k++) {
                                                               for (int k = 0; k < l; k++) {
                                                                 i-foreach (point i : Ie(R, g)) phased {
           S2:
           next; } } } } }
                                                                  S2; }
                                                                 next; // Contracted
```

Figure 10: Applying our iterative transformation framework on the strip-mined code in Figure 8. The changes in each step are shown in bold face.

```
finish {
  ph = new phaser(); // SIG_WAIT mode by default
  foreach (point g: Ig(R)) phased(ph) {
    for (int j = 0; j < m; j++) {
      for (point i : Ie(R, g)) {
         S1; }
      next;
    if (array[j] != 0) {
        for (int k = 0; k < 1; k++) {
          for (point i : Ie(R, g)) {
                S2; }
                next; } }
</pre>
```

Figure 11: The chunked code for the running example shown in Figure 5.

Finally, Rule 4 (Next Contraction) is a new transformation that is specific to clocks and phasers. If we have an i-foreach loop that contains only a next statement, then we can replace it by a single next statement provided that its region is non-empty. This is because the only visible effect of an "i-foreach next" statement is synchronization with other activities, which can be achieved just as well by a single next statement.

Figure 10(a-d) shows the results of applying our transformations on the strip-mined code in Figure 8. First, Figure 10(a) shows the result of interchanging the i-foreach loop with the sequential for-j loop. Next, Figure 10(b) shows the result of distributing the i-foreach into three new i-foreach loops. Then, Figure 10(c) shows the result of Next Contraction and Loop Unswitching to move the third i-foreach further inwards. Finally, Figure 10(d) shows the result of Loop Interchange, Loop Distribution, and Next Contraction transformations, after which our desired goal of isolating all next statements have been achieved.

3.3 Serialization

The job of Serialization is to confirm that no i-foreach statement contains a next, and (if so) to serialize all the i-foreach constructs. Figure 11 shows the generated code after the serialization pass is performed on the transformed code in Figure 10(d). A quick comparison with the original code in Figure 5 confirms that foreach chunking is not a straightforward transformation in general. Likewise, Figure 12 shows the correctly chunked transformation of the example in Figure 2 from Section 1, unlike the naive incorrect version in Figure 3.

4. EXTENSIONS FOR EXCEPTIONS

In this section, we discuss rules to perform loop-chunking transformations in the presence of exceptions. The rules in this section are presented in the context of the X10 v1.5 exception model (which in turn builds on the Java exception model), but the overall approach should be relevant to other languages with exception semantics (such as C++).

As discussed in section 2.1, an uncaught exception thrown inside an async statement terminates the async but not its parent activity. The enclosing finish statement captures all the exceptions that are thrown inside its body, aggregates them into a MultiException data structure and throws this collection instead of a single exception – which unless han-

```
delta = epsilon+1; iters = 0;
phaser ph = new phaser(single);
foreach ( point[jj] : [1:n:S] ) phased(single(ph)) {
  while ( delta > epsilon ) {
    for (int j = jj ; j <= min(jj+S-1,n) ; j++) {
        newA[j] = (oldA[j-1]+oldA[j+1])/2.0 ;
        diff[j] = Math.abs(newA[j]-oldA[j]);
    }
    next { // barrier with single statement
        delta = diff.sum(); iters++;
        temp = newA; newA = oldA; oldA = temp;
    }
    // while
} // parallel for</pre>
```

Figure 12: Correctly chunked transformation of X10 example from Figure 2.

dled will in turn terminate the activity invoking the finish. Exceptions thrown in the iterations of a foreach loop are handled similarly (does not impact the execution of other iterations), as each iteration of the foreach statement can be viewed as an independent async statement.

We first discuss the exception semantics of the i-foreach statement. An i-foreach statement is a temporary placeholder for a sequential for loop. Any exception thrown in a sequential for loop typically terminates the loop. However, since the for loop generated from the i-foreach statement is originally part of a foreach statement, we must execute each iteration of the i-foreach regardless of exceptions thrown in other iterations. Thus, we define the exception semantics of the i-foreach as follows: all the exceptions thrown by different iterations of the i-foreach are thrown as independent asynchronous exceptions i.e., are inserted into the MultiException collection collected at the explicit IEF (Immediately Enclosing Finish) instance for the i-foreach (ignoring implicit finish operations in i-foreach statements).

We follow the same overall approach as shown in Figure 4 even in the presence of exceptions. We however modify the rules for some of the transformations. Figure 13 presents the modified rules to handle exceptions, which are also briefly discussed below. As we can see, the rules have now become more complicated than the rules in Figure 9, thereby underscoring the value of performing these transformations automatically with a compiler rather than depending on programmers to implement these transformations by hand.

Strip mining: We re-use the strip mining rule presented in Figure 7; the exception semantics of the i-foreach statement guarantees correct translation, keeping in mind that the implicit finish in an i-foreach does not collect exceptions like an explicit finish.

Loop interchange: Loop interchange (Rule 1) requires special handling in the presence of exceptions since an exception thrown in the original inner for loop terminates the rest of the iterations of the for loop, but does not impact other iterations of the i-foreach loop. Thus, in the transformed program, for any iteration of the outer sequential for loop, the inner i-foreach should be invoked at program point Q only if no exception was thrown by any of the previous sequential iterations while executing the activity at point Q. We capture this behavior by maintaining a region of points

```
1. Loop interchange:
                                              boolean c; Exception EX = null;
                                              try {s1; c = e;}
                                                 catch (Exception ex) {EX = ex; c = false;}
                                              if (EX \neq null) foreach (p: Ie(R, g)) throw EX;
                                              Region newR = new Region(Ie(R, g));
                                                 Exception [] exArr = new Exceptions[newR.size()];
                                              for (;c;) {
                                                 for (q: newR) if (exArr[q] \neq null) newR.remove(q);
 i-foreach (p: Ie(R, g)) phased
                                                 i-foreach (p: newR) phased {
   for (s1;e;s2)
                                                 // might have to do renaming
   // s1, e, s2 don't depend on p
                                                    try {
                                                      S;
                                                      s2; c = false; c = e;
                                                     } catch (Exception e) {exArr[p] = e; }
                                              }
                                              foreach (p: Ie(R, g))
                                                 if (exArr[p] \neq null)
                                                   throw exArr[p];
2. Loop unswitching:
                                              boolean c; Exception EX = null;
 i-foreach (p: Ie(R, g)) phased
                                              try {c = e;}
                                                 catch (Exception ex) {EX = ex; c = false;}
   if (e)
    // e doesn't depend on p and
                                              if (EX \neq null) foreach (p: Ie(R, g)) throw EX;
    // is side effect free
                                              if (c)
                                                 i-foreach (p: Ie(R, g)) phased
3. Loop unswitching (try-catch):
                                              try {
                                                 finish i-foreach (p: Ie(R, g)) phased
                                              } catch (MultiException e) {
                                                   Region newR = new Region();
                                                   for (p: Ie(R, g)) {
                                                     ex = e.exceptions[p];
 i-foreach (p: Ie(R, g)) phased
                                                     if (ex \neq null && ex instanceof E)
   try {
                                                       newR.add(p);
       S1
   } catch (E e) S2
                                                   i-foreach (p: newR) phased {
                                                       Exception e = e.exceptions[p];
                                                       S2
                                                   foreach (Exception ex: e.exceptions())
                                                     if (ex \neq null && !(ex instanceof E)) {throw ex;}
4. Loop distribution:
                                              Exception exArr[] = new Exception [R.size()];
                                              boolean exFlag[] = new boolean [R.size()];
                                              i-foreach (p: Ie(R, g)) phased
 i-foreach (p: Ie(R, g)) phased {
                                                 try {S1}
   S1;
                                                   catch (Exception e) {exFlag[p] = true; throw e;}
   S2
                                              Region newR = new Region();
                                              for (p: Ie(R, g)) if (!exFlag[p]) newR.add(p);
                                              i-foreach (p: newR) phased
                                                   S2;
5. Next-Contraction
 i-foreach (p: Ie(R, g)) phased
                                              next
   next
```

Figure 13: Rules for loop interchange, unswitching, distribution, and next contraction in the presence of exceptions.

(newR) for which no exception has been thrown. For any exception thrown, it is stored in an array and after the whole loop is executed, the contents of the array are individually thrown in an asynchronous manner.

Loop unswitching: If the predicate of the if statement is loop invariant and is side effect free, then we can compute the predicate outside the loop as shown in Rule 2.

Loop unswitching (try-catch): A try block within a foreach statement can be lifted out of the loop, by treating the try block and the catch block as two computations in sequence (the catch block is executed conditionally). We have to catch all the exception that might be thrown in the try-block. We do so, by first unswitching and then enclosing the inner i-foreach with a finish statement. As shown in Rule 3, any exception thrown in S1 is caught by the finish and is thrown as a MultiException. In the catch statement, we analyze the MultiException, and execute S2 inside a i-foreach loop over all the points for which we had caught an exception while executing S1 (newR). All the exceptions that are not caught by the catch-clause (exception not of type E) are thrown to the next level.

Loop distribution: Given the body of a foreach loop to be {S1; S2}, after the loop distribution, S2 is executed only by those iterations where S1 did not throw any exception. We create a new region newR to represent the collection of points that executed S1 normally (did not throw an exception outside) and use it to iterate over S2 as shown in Rule 4.

 $Next\ simplification:$ This rule is same as the rule presented in Figure 9.

Serialization of i-foreach statements must respect their exception semantics. We present below the rule for serialization in the presence of exceptions.

In each iteration, we catch any exception that is thrown and throw it asynchronously. This guarantees that we throw all the caught exceptions with the same semantics as the original foreach loop.

5. EXPERIMENTAL RESULTS

In this section, we present experimental results obtained using the compiler framework shown in Figure 14. The input programs are written in X10 (v 1.5) language [5] extended with phasers [20], but the approach is applicable to chunking of parallel loops with synchronization in other languages as well. We modified the Polyglot-based front-end for X10 [24] to emit a new Parallel Intermediate Representation (PIR) extension to the Jimple intermediate representation in the SOOT bytecode analysis and transformation framework [22]. The PIR includes explicit constructs for parallel operations such as foreach, async and finish. The transformations described in Section 3 are performed in the PIR Analysis & Optimization component, after which the PIR is translated to Java bytecodes. The transformed Java class files are executed using the X10 runtime based on the ThreadPoolExecutor utility from the java.util.concurrent library [2].

In this section, we report results for the 11 benchmarks listed in Table 1. The asterisk-ed benchmarks contain foreach loops with phaser next operations³; compiler analysis was

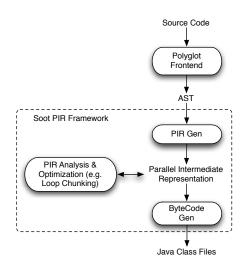
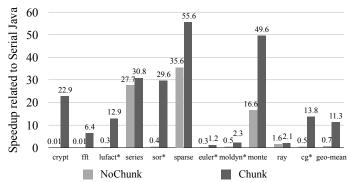


Figure 14: Soot-based PIR Compiler Framework



* Benchmarks with an asterisk have next operations within foreach loops

Figure 15: Speedup for JGF Benchmarks with Automatic Chunking for 64 threads on an UltraSPARC T2 SMP

necessary to establish the absence of next operations for the other benchmarks. All results were obtained on a 64-way (8 cores × 8 threads per core) 1.2 GHz UltraSPARC T2 (Niagara 2) with 32 GB main memory running Solaris 10, using a Java 5 Runtime Environment (build 1.5.0_12-b04) with Java HotSpot Server VM (build 1.5.0_12-b04, mixed mode) and the "-Xms1000M -Xmx1000M" options to set the heap size to 1GB. For all runs, the main program was extended with a 30-iteration loop within the same Java process, and the best of the 30 times was reported in each case so as to reduce the impact of JIT compilation time in the performance results, in accordance with the methodology reported in [9]. For the X10 runtime options, -NUMBER_OF_LOCAL_PLACES was set to 1 and -INIT_THREADS_PER_PLACE was set equal to the number of worker threads for which the measurement was being performed.

5.1 Performance Results for Automatic Chunking of Foreach Loops

In this section, we present results on a 64-way Sun Ultra-SPARC T2 server for the following variants of each benchmark:

• Serial. Sequential Java version without any parallel con-

³In most cases, next was used as a barrier, but in one case (SOR), next was used for point-to-point synchronization as described in [20].

Benchmark	Source Benchmark Suite	Data Size
Crypt, FFT, LUFact*, Series	Java Grande Forum (JGF) Benchmarks v2.0 Section 2	Size C (largest)
SOR*, SparseMatmult	JGF Benchmarks thread v1.0 Section 2	Size C (largest)
Euler*, MonteCarlo, RayTracer	JGF Benchmarks v2.0 Section 3	Size B (largest)
MolDyn*	JGF Benchmarks v2.0 Section 3	Size A(smallest)
CG*	Nas Parallel Benchmarks	Size A (between sizes S,W,A,B,C)

Table 1: List of benchmarks

Figure 16: LUFact kernel loop before chunking

Figure 17: LUFact kernel loop after chunking

structs from the original benchmark release. This version is used as the baseline for all speedup results.

- NoChunk. Fine-grained parallel X10 version using the finish, foreach and next statements. As described in [5], this corresponds to a high productivity variant for single place execution.
- Chunk. This version is the result of automatic compiler transformation of the NoChunk version using the foreach loop chunking transformations described in Section 3. A simple static chunking policy (one contiguous chunk per processor) was used in all cases. The next section includes hand-coded results for alternate chunking policies for two benchmarks.

Figure 15 shows the speedup obtained for the all benchmarks shown in Table 1 with 64 threads. The data size used for each benchmark is shown in the last column of Table 1; we used the largest input size for all benchmarks except MolDyn and CG for which the NoChunk versions could not complete execution for the largest sizes. We measured speedup relative to the original Java serial version. As shown in the chart, the fine-grained NoChunk case can lead to significant overhead — for 8 of 11 benchmarks (Crypt, FFT, LUFact, SOR, Euler, MolDyn, RayTracer, CG) the NoChunk parallel version on 64 threads was much slower than the Serial version on 1 thread, by three orders of magnitude in one case. This is not surprising, since the relative overhead of spawning each iteration of a foreach loop as a new activity can be prohibitively large for fine-grained foreach loops. The geometric mean of all speedups for the NoChunk case is 0.73×. On the other hand, the Chunk case shows that the techniques introduced in this paper are very effective in eliminating this overhead. None of the benchmarks showed a slowdown, and the overall geometric mean speedup is 11.3×. The geometric mean speedup among the benchmarks that had next phaser operations was 6.8×. Among all the benchmarks the largest gap was observed for Crypt where the Chunk version ran more than $2180 \times$ faster than the NoChunk case. Figure 16 shows the kernel parallel loop of LUFact, which includes two barrier operations. Here, n is 2000 with Size C, and the speedup without foreach chunking is less than one due to huge barrier overhead among 1999 activities. The foreach chunking transformation shown in Figure 17 reduced # activities to the optimal number and obtained 12.9× speedup. SOR, Euler, MolDyn and CG also have next operations in the loop bodies of foreach loops.

5.2 Hand-coded Comparison of Different Chunking Policies

The previous section presented performance results for automatic chunking of foreach loops using a fixed static chunking policy. It is well known that different chunking policies may be best for different parallel loops depending on the load imbalance and locality across different iterations. In this section, we use hand-coded transformations to explore the impact of chunking policy on two benchmarks, LUFact and MolDyn. In future work, we plan to obtain these measurements automatically by allowing the programmer to annotate a foreach loop with a desired chunking policy (as in OpenMP), and by also investigating automatic selection of chunking policies in the compiler.

These hand-coded performance results include some additional transformations that we expect to include in a future version of our compiler. Loop-invariant-code-motion (LICM) moves the loop invariant code out of the foreach loop. Given the example in Figure 10(c), if all of the operands

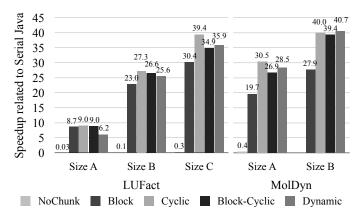


Figure 18: Speedup for JGF LUFact and Mol-Dyn with Hand-Optimized Chunking Policies for 64 threads on an UltraSPARC T2 SMP

in S1 are loop invariants in the i-foreach loop, then S1 can be moved outside the i-foreach and its surrounding i-foreach can be eliminated as an empty loop. Another optimization performed in the hand-coded version is contraction of reduction arrays as follows:

```
foreach ( point i : R ) phased(ph) {
   A[i] = foo(i);
   next {    sum = A.sum;  }
   ... }
```

If the compiler can recognize that array A is only used in a reduction, a future extension to the foreach chunking transformation should be able to replace A by a new array whose size is equal to # processors.

We hand-coded four different scheduling policies to evaluate the impact of chunking on them:

- 1. **Block.** Statically divide the N iterations into P chunks for P processors (one chunk of contiguous iterations per processor) as in the Chunk case in the previous section. The main difference between Chunk and Block is that the Block version includes the additional hand-coded optimizations listed above.
- 2. Cyclic. Perform a cyclic partitioning of the iterations into P chunks of non-contiguous iterations, so that each chunk executes iterations that are P apart.
- 3. **Block-cyclic.** Divide the iteration space into $H \times P$ contiguous chunks, where H is the number of "hops" and the block size for each chunk is $N/(H \times P)$. These $H \times P$ chunks are assigned to the P processors in a cyclic manner. We used H=4 for the results in this section.
- 4. **Dynamic.** Create one activity per processor at the outer level, but enable the activities to dynamically share chunks of parallel loop iterations, with chunk size $N/(H \times P)$ and H=4 as in the Block-cyclic case. This is analogous to worksharing parallel loops in an SPMD execution model except that the Dynamic policy is augmented with locality improvement techniques in our implementation where each activity keeps a history of executed chunks and accessed data, and uses it to take the next chunk.

Figure 18 shows the speedup for the JGF LUFact and MolDyn benchmarks when using all 64 threads on an Ultra-SPARC II. As we saw earlier, the versions without foreach chunking are slower than serial execution for LUFact and MolDyn (even with the hand-coded optimizations). Further,

the NoChunk version did not complete for Size B for MolDyn due to OutOfMemory and other runtime errors resulting from the creation of too many activities. On the other hand, all the chunked versions show good speedup. The speedups relative to the serial Java version for LUFact with Size C (the largest size for LUFact) are $30.4\times$ for Block, $39.4\times$ for Cyclic, $34.9\times$ for Block-Cyclic, and $35.9\times$ for Dynamic. It is not surprising that Cyclic yields the best performance for LUFact, since the work in each parallel iteration is embodied in a triangular sequential loop. However, the other policies deliver reasonable performance as well.

For MolDyn, the speedups relative to the serial Java version for Size B (the largest size for MolDyn) are $27.9\times$ for Block, $40.0\times$ for Cyclic, $39.4\times$ for Block-Cyclic, and $40.7\times$ for Dynamic. The Dynamic policy worked best for MolDyn because it was able to address load balancing issues without compromising data locality.

6. RELATED WORK

There has been a lot of past work on reducing synchronization and thread creation overheads. These include SP-MDization [3], synchronization optimizations [8], and barrier elimination [21]. Researchers have studied the impact of loop chunking on different parameters of interest. Hari et al. [12] use loop chunking as a means of efficient scheduling temperature-aware code. OpenMP 3.0 [17] supports different loop scheduling policies, as specified by the programmer, in parallel loops. However, the OpenMP language framework is restrictive in its support for synchronization operations inside parallel loops.

There has also been significant interest in loop scheduling [14]. Akin to chunking, loop scheduling has been directed at reducing the number of overall barriers and thread creation overheads. The loop scheduling techniques also use different loop transformation techniques (for example, loop interchange and loop coalescing) to identify chunks of iterations that can be scheduled together. Loop chunking can be seen as a special version of loop scheduling where all the iterations scheduled to be executed on the same processor are executed sequentially.

We are not aware of any past work that supports chunking of parallel loops in the presence of synchronization, as in this paper, for languages that support dynamic parallelism with fine grain synchronization.

7. CONCLUSIONS AND FUTURE WORK

In this paper, we presented a transformation framework for chunking parallel loops in the presence of synchronization operations and exceptions. We presented a systematic method that extends past classical loop transformation techniques to automate the loop chunking procedure in a safe way. These transformations resulted in reduced synchronization and scheduling overheads, thereby improving performance and scalability. Our experimental results for 11 benchmark programs on an UltraSPARC II multicore processor showed a geometric mean speedup of $0.52\times$ for the unchunked case and $9.59\times$ for automatic chunking using the techniques described in this paper. This wide gap underscores the importance of using these techniques in future compiler and runtime systems for programming models with lightweight parallelism.

We have also identified opportunities for further refinement of the approach presented in this paper. As mentioned earlier, our framework follows an all-or-nothing approach with respect to transforming i-foreach loops; however, this could be extended to transform selected i-foreach loops and leave the others unchanged. In this work, we also assumed that all programmer-specified conditions guarding a next statement are *invariant* in the initial foreach loop, even though we could handle cases when a next statement is guarded by implicit exception conditions. An extension that supports arbitrary conditional expressions as guards for next operations is a challenging subject for future research.

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