
COMP 322: Fundamentals of Parallel Programming

Lecture 12: Iteration Grouping (Chunking), Barrier Synchronization

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<https://wiki.rice.edu/confluence/display/PARPROG/COMP322>



Solution to Worksheet #11: One-dimensional Iterative Averaging Example

1) Assuming $n=9$ and the input array below, perform one iteration of the iterative averaging example by only filling in the blanks for odd values of j in the `myNew[]` array. Recall that the computation is “`myNew[j] = (myVal[j-1] + myVal[j+1])/2.0;`”

index, j	0	1	2	3	4	5	6	7	8	9	10
myVal	0	?	0.2	?	0.4	?	0.6	?	0.8	?	1
myNew	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1

2) Will the contents of `myVal[]` and `myNew[]` change in further iterations, after `myNew` above in 1) becomes `myVal[]` in the next iteration?

No, this represents the converged value (equilibrium/fixpoint).



Outline of Today's Lecture

- Iteration Grouping (Chunking)
- Barrier Synchronization



forall vs. forallChunked APIs (Recap)

- `forall(int s0, int e0, HjProcedure<java.lang.Integer> body)`
- `forall(0, 7, (i) -> BODY(i)); // 8 tasks`

Task 0	Task 1	Task 2	Task 3	Task 4	Task 5	Task 6	Task 7
BODY(0)	BODY(1)	BODY(2)	BODY(3)	BODY(4)	BODY(5)	BODY(6)	BODY(7)

- `forallChunked(int s0, int e0, int chunkSize, edu.rice.hj.api.HjProcedure<java.lang.Integer> body)`
- `forallChunked(0, 7, 2, (i) -> BODY(i)); // 4 tasks`

Task 0		Task 1		Task 2		Task 3	
BODY(0)	BODY(1)	BODY(2)	BODY(3)	BODY(4)	BODY(5)	BODY(6)	BODY(7)

- **Chunking is a special case of “iteration grouping”**



One-Dimensional Grouping (Pseudocode)

forall (i : [0:n-1]) s1 \Rightarrow

forall (g : [0:ng-1])

for(i : myGroup(g, [0:n-1], ng)) s1

where

- ng = number of groups
- g = group id (index variable of outer forall)
- myGroup(g, [0:n-1], ng) = region corresponding to group g
 - No requirement that iterations in a group be contiguous!



Two Common Groupings

- Block grouping (a.k.a. "chunking")

Task 0		Task 1		Task 2		Task 3	
BODY(0)	BODY(1)	BODY(2)	BODY(3)	BODY(4)	BODY(5)	BODY(6)	BODY(7)

- Cyclic grouping

Task 0		Task 1		Task 2		Task 3	
BODY(0)	BODY(4)	BODY(1)	BODY(5)	BODY(2)	BODY(6)	BODY(3)	BODY(7)



HJlib myGroup() method for 1D Grouping

```
1.     public static HjRegion1D myGroup(final int groupId,
2.         final HjRegion1D hjRegion1D, final int groupSize) {
3.         final int lower0 = hjRegion1D.lowerLimit(0);
4.         final int upper0 = hjRegion1D.upperLimit(0);
5.         final int range0 = upper0 - lower0 + 1;
6.         final int increment0 = (range0 / groupSize) +
7.             (range0 % groupSize == 0 ? 0 : 1);
8.         final int start0 = (groupId * increment0) + lower0;
9.         final int end0 = Math.min(upper0,
10.             start0 + increment0 - 1);
11.         return newRectangularRegion1D(start0, end0);
12.     }
```



Example Use of 1D myGroup API

```
1. HjRegion1D iterSpace = newRectangularRegion1D(0,N-1);
2. forall(0, tasks - 1, (t) -> {
3.     HjRegion.HjRegion1D myGroup =
4.         myGroup(t, iterSpace, tasks);
5.     forseq(myGroup, (i) -> {
6.         for (int j = 0; j < N; j++)
7.             for (int k = 0; k < N; k++)
8.                 c[i][j] += A[i][k] * B[k][j];
9.     }); // forseq
10. }); // forall
```



Pros & Cons of Chunked vs. Group APIs

- `forallChunked`
 - Pro: efficient performance (no call to `forseq`)
 - Con: grouping policy is determined by library
- `myGroup` (1D version):
 - Pro: grouping interface exposed to programmer
 - Con: explicit `forseq` is source of complexity and inefficiency
- `myGroup` (2D version):
 - Pro: programmer can control number of groups in each dimension
 - Con: explicit `forseq` is source of complexity and inefficiency



Two-Dimensional Grouping (Pseudocode)

```
forall ([i,j] : [0:n-1,0:n-1]) s1  =>
forall ([g0,g1] : [0:ng0-1,0:ng1-1])
  for([i,j] : myGroup([g0,g1], [0:n-1,0:n-1],
                      ng0, ng1) s1
```

where

- $ng0 * ng1$ = **totalnumber of groups**
- $g0, g1$ = **two-dimensional group id**
- $myGroup([g0, g1], [0:n-1, 0:n-1], ng0, ng1)$ = **region corresponding to group $g0, g1$**



HJlib myGroup() method for 2D Grouping

```
1.  public static RectangularRegion2D myGroup(  
2.      final int groupId0, final int groupId1,  
3.      final HjRegion2D hjRegion2D,  
4.      final int groupSize0, final int groupSize1) {  
  
6.      final int[] lowerLimits = hjRegion2D.lowerLimits();  
7.      final int[] upperLimits = hjRegion2D.upperLimits();  
  
9.      final int lower0 = lowerLimits[0];  
10.     final int upper0 = upperLimits[0];  
11.     final int range0 = upper0 - lower0 + 1;  
12.     final int increment0 = (range0 / groupSize0) + (range0 % groupSize0 == 0 ? 0 : 1);  
  
14.     final int lower1 = lowerLimits[1];  
15.     final int upper1 = upperLimits[1];  
16.     final int range1 = upper1 - lower1 + 1;  
17.     final int increment1 = (range1 / groupSize1) + (range1 % groupSize1 == 0 ? 0 : 1);  
  
19.     final int start0 = (groupId0 * increment0) + lower0;  
20.     final int end0 = Math.min(upper0, start0 + increment0 - 1);  
  
22.     final int start1 = (groupId1 * increment1) + lower1;  
23.     final int end1 = Math.min(upper1, start1 + increment1 - 1);  
  
25.     return newRectangularRegion2D(start0, end0, start1, end1);  
26. }  

```



Example Use of 2D myGroup API

```
1. HjRegion2D hjRegion = newRectangularRegion2D(0, N-1, 0, N-1);
2. final int grid1 = Math.sqrt(tasks);
3. final int grid2 = grid1;
4. assert(grid1*grid2==tasks, "tasks is not a perfect square?")
5. forall(0, tasks - 1, (t) -> {
6.     final int id1 = t / grid1;
7.     final int id2 = t % grid1;
8.     final RectangularRegion2D myGroup =
9.         myGroup(id1, id2, hjRegion, grid1, grid2);
10.    forseq(myGroup, (i, j) -> {
11.        computationKernel(A, B, C, N, i, j);
12.    }); // forseq
13. }); // forall
14.
```



k-dimensional Iteration Grouping (General approach in pseudocode)

- Assume that the forasync loop originally iterates over region r
`forall(r, (p) -> BODY(p)); // No. of tasks = r.size()`
- Assume that we have an int array, $nc = \{nc_0, nc_1, \dots\}$, for the desired number of chunks in each dimension
 - A good choice is to choose these values such that the product of $nc[0]*nc[1]*\dots = \text{Runtime.getNumOfWorkers}()$
- Assume that we have a helper method, `getChunk(id, r, nc)` that returns the iteration range for chunk pp as an HJ region
 - e.g., `getChunk([0,0], [0:99,0:99], {2,2}) = [0:49,0:49]`
-



Outline of Today's Lecture

- Iteration Grouping (Chunking)
- Barrier Synchronization



Hello-Goodbye Forall Example (Pseudocode)

```
forall (0, m - 1, (i) -> {  
    int sq = i*i;  
    System.out.println("Hello from task with square = " + sq);  
    System.out.println("Goodbye from task with square = " + sq);  
});
```

- **Sample output for m = 4**

```
Hello from task with square = 0  
Hello from task with square = 1  
Goodbye from task with square = 0  
Hello from task with square = 4  
Goodbye from task with square = 4  
Goodbye from task with square = 1  
Hello from task with square = 9  
Goodbye from task with square = 9
```



Hello-Goodbye Forall Example (contd)

```
forall (0, m - 1, (i) -> {  
    int sq = i*i;  
    System.out.println("Hello from task with square = " + sq);  
    System.out.println("Goodbye from task with square = " + sq);  
});
```

- Question: how can we transform this code so as to ensure that all tasks say hello before any tasks say goodbye?
- Statements in red below will need to be moved to solve this problem

Hello from task with square = 0

Hello from task with square = 1

Goodbye from task with square = 0

Hello from task with square = 4

Goodbye from task with square = 4

Goodbye from task with square = 1

Hello from task with square = 9

Goodbye from task with square = 9



Hello-Goodbye Forall Example (contd)

```
1. forall (0, m - 1, (i) -> {
2.   int sq = i*i;
3.   System.out.println("Hello from task with square = " + sq);
4.   System.out.println("Goodbye from task with square = " + sq);
5. });
```

- **Question:** how can we transform this code so as to ensure that all tasks say hello before any tasks say goodbye?
- **Approach 1:** Replace the forall loop by two forall loops, one for the hello's and one for the goodbye's

— **Problem:** Need to communicate local sq values from one forall to the next

```
1. // APPROACH 1
2. forall (0, m - 1, (i) -> {
3.   int sq = i*i;
4.   System.out.println("Hello from task with square = " + sq);
5. });
6. forall (0, m - 1, (i) -> {
7.   System.out.println("Goodbye from task with square = " + sq);
8. });
```



Hello-Goodbye Forall Example (contd)

- Question: how can we transform this code so as to ensure that all tasks say hello before any tasks say goodbye?

- Approach 2: insert a “barrier” between the hello's and goodbye's

- “next” statement in HJ's forall loops

```
1. // APPROACH 2
2. forallPhased (0, m - 1, (i) -> {
3.   int sq = i*i;
4.   System.out.println("Hello from task with square = " + sq);
5.   next(); // Barrier
6.   System.out.println("Goodbye from task with square = " + sq);
7. });
```

Phase 0

Phase 1

- **next** → each forall iteration suspends at next until all iterations arrive (complete previous phase), after which the phase can be advanced
 - If a forall iteration terminates before executing “next”, then the other iterations do not wait for it
 - Scope of next is the closest enclosing forall statement
 - Special case of “phaser” construct (will be covered later in class)



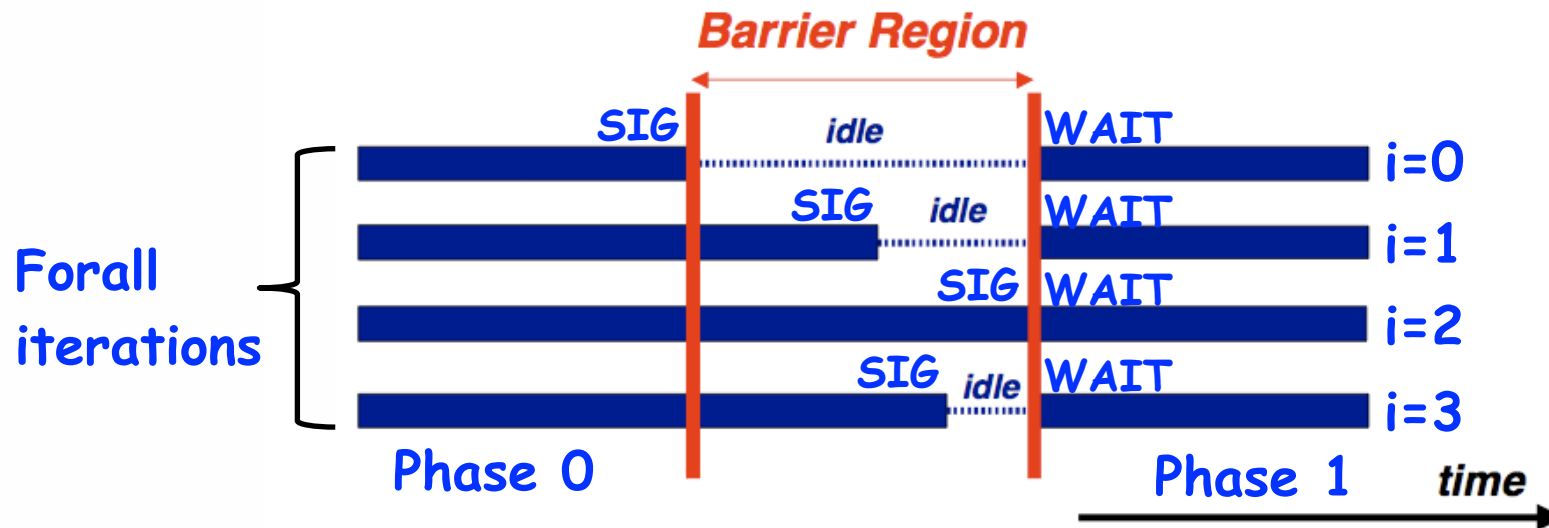
forallPhased API's in HJlib

(<http://www.cs.rice.edu/~vs3/hjlib/doc/edu/rice/hj/Module1.html>)

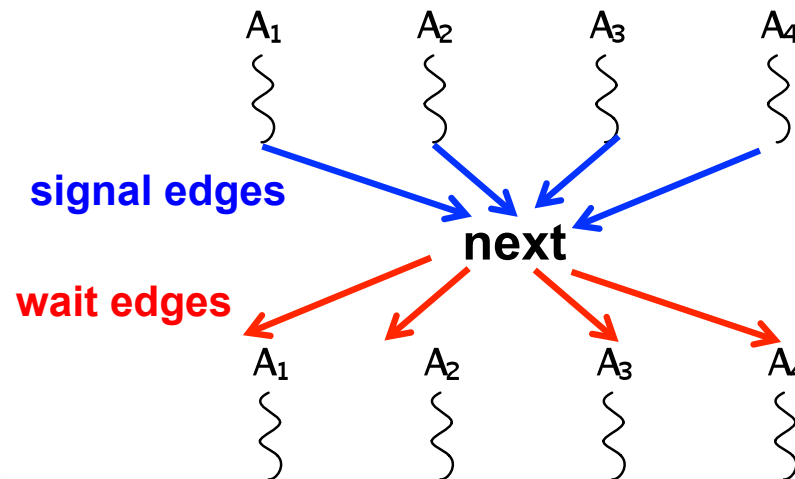
- `static void forallPhased(int s0, int e0, edu.rice.hj.api.HjProcedure<java.lang.Integer> body)`
- `static <T> void forallPhased(java.lang.Iterable<T> iterable, edu.rice.hj.api.HjProcedure<T> body)`
- `static void next()`
- **NOTE:**
 - All forallPhased API's include an implicit finish.
 - Calls to next() are only permitted in forallPhased() not in forall()



Impact of barrier on scheduling forall iterations



Modeling a next operation in the computation graph



Observation 1: Scope of synchronization for “next” is closest enclosing forall statement

```
1. forallPhased (0, m - 1, (i) -> {
2.   println("Starting forall iteration " + i);
3.   next(); // Acts as barrier for forall-i
4.   forallPhased (0, n - 1, (j) -> {
5.     println("Hello from task (" + i + "," + j + ")");
6.     next(); // Acts as barrier for forall-j
7.     println("Goodbye from task (" + i + "," + j + ")");
8.   } // forall-j
9.   next(); // Acts as barrier for forall-i
10.  println("Ending forall iteration " + i);
11.}); // forall-i
```



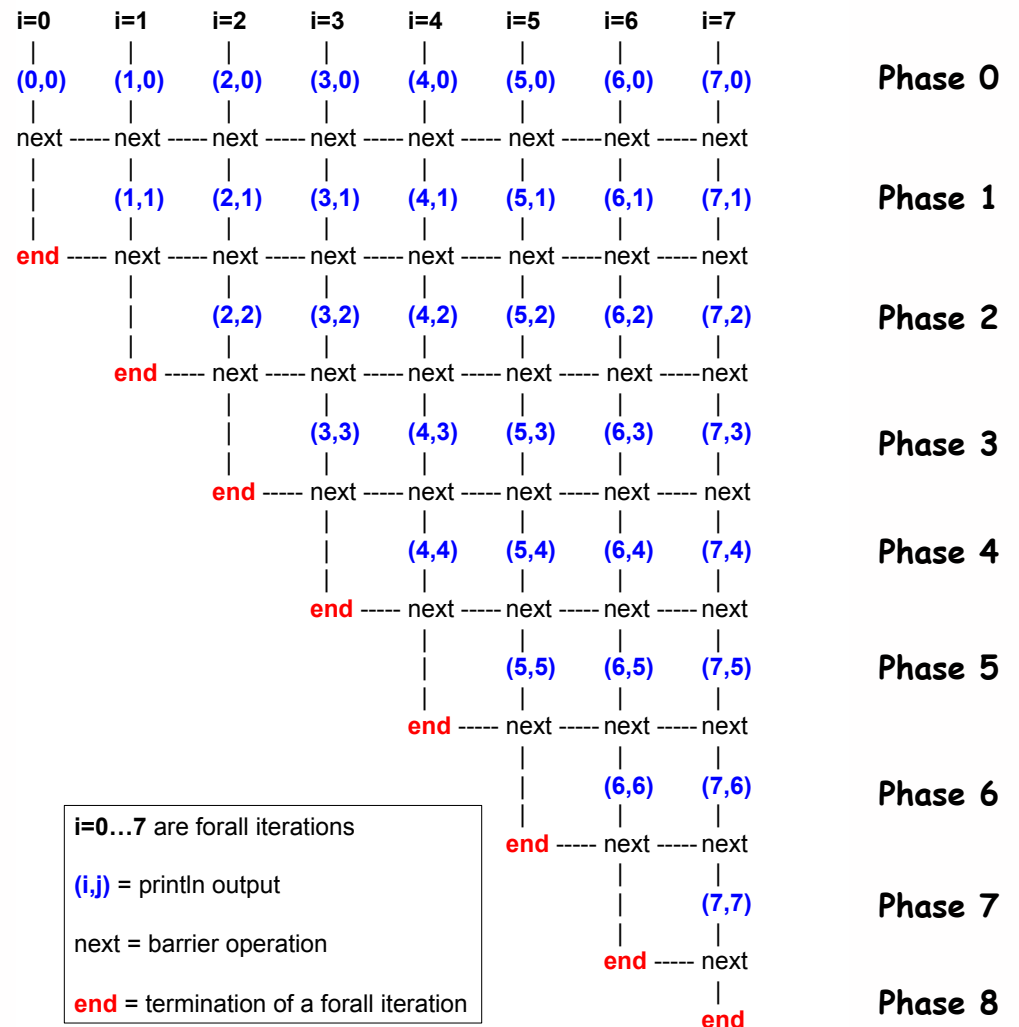
Observation 2: If a forall iteration terminates before “next”, then other iterations do not wait for it

1. `forallPhased (0, m - 1, (i) -> {`
 2. `forseq (0, i, (j) -> {`
 3. `// forall iteration i is executing phase j`
 4. `System.out.println("(" + i + "," + j + ")");`
 5. `next();`
 6. `});`
 7. `});`
- Outer forall-i loop has m iterations, 0...m-1
 - Inner sequential j loop has i+1 iterations, 0...i
 - Line 4 prints (task,phase) = (i, j) before performing a next operation.
 - Iteration i = 0 of the forall-i loop prints (0, 0), performs a next, and then terminates. Iteration i = 1 of the forall-i loop prints (1,0), performs a next, prints (1,1), performs a next, and then terminates. And so on.



Illustration of previous example

- Iteration $i=0$ of the forall- i loop prints $(0, 0)$ in Phase 0, performs a next, and then ends Phase 1 by terminating.
- Iteration $i=1$ of the forall- i loop prints $(1,0)$ in Phase 0, performs a next, prints $(1,1)$ in Phase 1, performs a next, and then ends Phase 2 by terminating.
- And so on until iteration $i=8$ ends an empty Phase 8 by terminating



Observation 3: Different forall iterations may perform “next” at different program points (barrier matching problem)

```
1. forallPhased (0, m-1, (i) -> {
2.     if (i % 2 == 1) { // i is odd
3.         oddPhase0(i);
4.         next();
5.         oddPhase1(i);
6.     } else { // i is even
7.         evenPhase0(i);
8.         next();
9.         evenPhase1(i);
10.    } // if-else
11. }); // forall
```

- Barrier operation synchronizes odd-numbered iterations at line 4 with even-numbered iterations in line 8
- next statement may even be in a method such as oddPhase1()



Worksheet #12: Forall Loops and Barriers

Name: _____

Netid: _____

Draw a “barrier matching” figure similar to slide 23 for the code fragment below.

```
1. String[] a = { "ab", "cde", "f" };
2. . . . int m = a.length; . . .
3. forallPhased (0, m-1, (i) -> {
4.     for (int j = 0; j < a[i].length(); j++) {
5.         // forall iteration i is executing phase j
6.         System.out.println("(" + i + "," + j + ")");
7.         next();
8.     }
9. });
```

